

23rd Summer School on PARALLEL COMPUTING

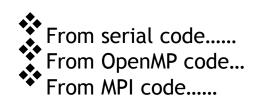
Hybrid Programming: MPI + OpenMP

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Hybrid parallelization...the Long and Winding Road







Hybrid parallelization...the Long and Winding road

✤ From serial code...





Hybrid parallelization...the Long and Winding road

From OpenMP code...





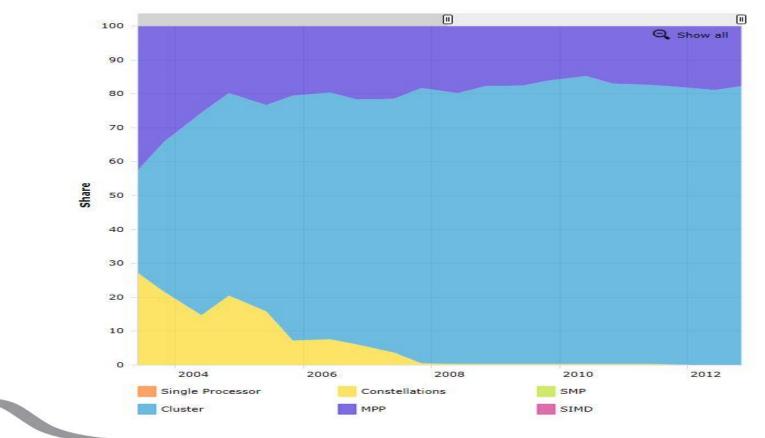
Hybrid parallelization...the Long and Winding road

From MPI code...



Architectural Trend

Top 500 historical view: clusters (and MPP) dominates HPC arena



Architecture - Systems Share

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Architectural Trend (cont.)

Top 500 historical view: the multicore age



Cores per Socket - Systems Share



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Architectural Trend (cont.)

- Multi-socket nodes with rapidly increasing core counts.
- Memory per core decreases.
- Memory bandwidth per core decreases.
- Network bandwidth per core decreases.
- Deeper memory hierarchy.

Which programming model is the best choice for this architectural trend ?



Programming model

Which programming model is the best choice for this architecture?

- MPI is the de-facto standard for distributed memory architectures
- in principle, MPI library is supposed to scale up to 10k cores and over....
- ...but the MPI model (*flat*) is not guaranteed to match with this architecture for any kind of application!



Programming model

Which programming model is the best choice for this architecture?

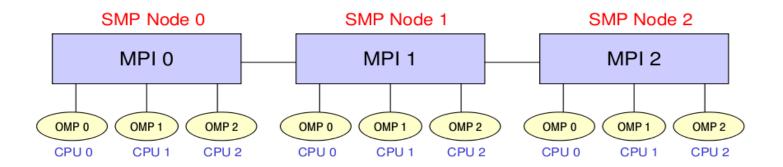
- OpenMP is the de-facto standard for shared-memory architectures (SMP and Multisocket nodes).
- OpenMP standard is robust, clear and sufficently easy to implement but is supposed not to scale up to hundreds of cores!
- What about MPI+OpenMP?





The Hybrid model

- Logical view: multi-node SMP (Symmetric Multiprocessor).
- MPI between the nodes via node interconnect
- OpenMP (the standard for shared memory parallel programming) inside of the SMP nodes





MPI vs. OpenMP

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Pure MPI Pro:

- High scalability
- High portability
- No false sharing
- Scalability out-of-node

Pure MPI Con:

- Hard to develop and debug.
- Explicit communications
- Coarse granularity
- Hard to ensure load balancing

Pure OpenMP Pro:

- Easy to deploy (often)
- Low latency
- Implicit communications
- Coarse and fine granularity
- Dynamic Load balancing

Pure OpenMP Con:

Only on shared memory machines Intranode scalability Possible data placement problem Undefined thread ordering

Why Hybrid?

- MPI+OpenMP hybrid paradigm is the trend for clusters with SMP architecture.
- Elegant in concept: use OpenMP within the node and MPI between nodes, in order to have a good use of shared resources.
- Avoid additional communication within the MPI node.
- OpenMP introduces fine-granularity.
- Two-level parallelism
- Some problems can be reduced by lowering MPI procs number
- If the problem is suitable, the hybrid approach can have better performance than pure MPI or OpenMP codes.

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Avoid additional communication within the MPI node

In the pure MPI model each process needs to allocate some extra memory to manage communications and MPI environment Supposing to use threads within node : Smaller number of MPI processes Fewer messages, larger message size

Example: one node having 8 cores and 32 GB. Pure MPI and Hybrid:

Pure MPI: 8 MPI process, 4 GB for each (parallelism is 8) Pure MPI: 1 MPI process, 32 GB (serial) Hybrid: 1 MPI process, 8 threads. 32 GB <u>shared</u> per process, 4 GB per thread. (parallelism is 8)



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OpenMP introduces fine-granularity

- Loop-based parallelism (just a set of directives in your code)
- Task construct (OpenMP 3.0): powerful and flexible
- Dynamic and guided scheduling (load balancing)
- Without additional software effort
- Without explicit data movement (MPI's drawback)

Why Hybrid?

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Two level parallelism

- Parallelism across SMP nodes, single node equipped with m sockets and n cores per socket.
- To be assigned: the number of MPI process and the (optimal) number of threads per MPI process.
- Heuristics:
- (often) n threads per MPI process
- (sometimes) n/2 threads per MPI process
- (seldom) 2n threads per MPI process
- No golden rule, application and hardware dependent

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Why Hybrid?

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Some problems can be reduced By lowering MPI procs number

- Memory consumption can be alleviated by a reduction of replicated data on MPI level
- Speedup limited due to algorithmic problem can be solved
- MPI scaling problems (expecially to high number of cores) can be significantly reduced
- MPI scaling problems can be solved by a reduced aggregated message size (compared to pure MPI)

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Why mixing MPI and OpenMP code can be slower?

- OpenMP has lower scalability because of locking resources while MPI has not potential scalability limits.
- All threads are idle except ones during an MPI communication
 - Need overlap computation and communication to improve performance
 - Critical section for shared variables update
- Overhead of thread creation
- Cache coherency and false sharing.
- Pure OpenMP code is generally slower than pure MPI code
- Fewer optimizations by OpenMP compilers compared to MPI



Cache coherency and False sharing

It is a side effects of the cache-line granularity of cache coherence implemented in shared memory systems.

- The cache coherency implementation keep track of the status of cache lines by appending state bits to indicate whether data on cache line is still valid or • outdated.
- Once the cache line is modified, cache coherence notifies other caches holding a copy of the same line that its line is invalid.
 If data from that line is needed, a new updated copy must to be fetched.



Cache coherency and False sharing

#pragma omp parallel for shared(a)
schedule(static,1)
for (int i=0; i<n; i++)
 a[i] = i;</pre>

Suppose that each cache line consist of 4 elements and you are using 4 threads

Each thread store:

Assuming that a[0] is the beginning of the cache line, we have 4 false sharing The same for a[4]...,a[7]

Thread ID Stores		
0	a[0]	
1	a[1]	
2	a[2]	
3	a[3]	
0	a[4]	

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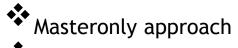
Cache coherency and False sharing

The problem is that *state bits* do not keep track of which part of the line is outdated, but indicates the whole line
 As a result, when two threads update different data elements in the same cache line, they interfer with each other
 Solving:
 Using private data instead of shared data
 Padding





Hybrid parallelization Roadmap



...if works...

...then, try to use MPI inside parallel regions with a tread-safe MPI



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Hybrid code (Masteronly)

```
call MPI_INIT (ierr)
call MPI_COMM_RANK (...)
call MPI_COMM_SIZE (...)
... some computation and MPI communication
call OMP_SET_NUM_THREADS(4)
!$OMP PARALLEL
!$OMP DO
do i=1,n
... computation
enddo
!$OMP END DO
!$OMP END DO
!$OMP END PARALLEL
... some computation and MPI communication
call MPI_FINALIZE (ierr)
```

CINEC.

Hybrid code (Masteronly)



The various MPI implementations differs in levels of thread-safety Advantages of Masteronly: No message passing inside of SMP nodes Simplest hybrid parallelization (easy to implement, debug, ...) Major problems: Summer School on

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All other threads are sleeping while master thread communicates

Use of internode bandwidth satisfactory?

Thread-safe MPI is required



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MPI_INIT_Thread support (MPI-2)

- MPI_INIT_THREAD (required, provided, ierr)
 - IN: required, desired level of thread support (integer).
 - OUT: provided, provided level (integer).
 - provided may be less than required.
- Four levels are supported:
 - * MPI_THREAD_SINGLE: Only one thread will runs. Equals to MPI_INIT.
 - MPI_THREAD_FUNNELED: processes may be multithreaded, but only the main thread can make MPI calls (MPI calls are delegated to main thread)
 - MPI_THREAD_SERIALIZED: processes could be multithreaded. More than one thread can make MPI calls, but only one at a time.
 - * MPI_THREAD_MULTIPLE: multiple threads can make MPI calls, with no restrictions.



MPI_INIT_Thread support (MPI-2)

- The various implementations differs in levels of thread-safety
- If your application allow multiple threads to make MPI calls simultaneously, whitout MPI_THREAD_MULTIPLE, is not thread-safe
- Using OpenMPI, you have to use -enable-mpi-threads at configure time to activate all levels.
- Higher level corresponds higher thread-safety. Use the required safety needs.

MPI_THREAD_SINGLE

Equivalent to Hybrid Masteronly:

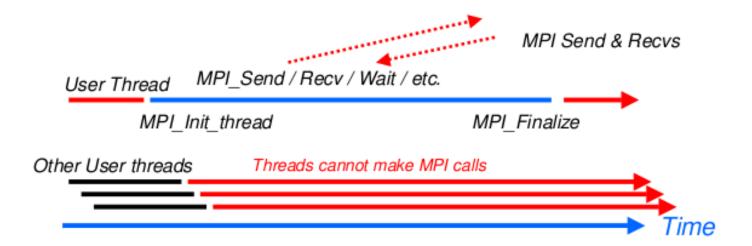
```
!$OMP PARALLEL DO
do i=1,10000
a(i)=b(i)+f*d(i)
enddo
!$OMP END PARALLEL DO
call MPI_Xxx(...)
!$OMP PARALLEL DO
do i=1,10000
x(i)=a(i)+f*b(i)
enddo
!$OMP END PARALLEL DO
```

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```
#pragma omp parallel for
    for (i=0; i<10000; i++)
    { a[i]=b[i]+f*d[i];
    }
/* end omp parallel for */
    MPI_Xxx(...);
#pragma omp parallel for
    for (i=0; i<10000; i++)
    { x[i]=a[i]+f*b[i];
    }
/* end omp parallel for */
```

MPI_THREAD_FUNNELED

Only the master thread can do MPI communications.





MPI_THREAD_FUNNELED

- MPI calls:
- □ outside the parallel region.
- □ inside the parallel region with "omp master".

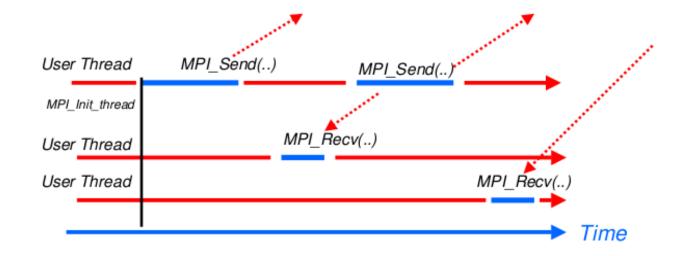
!\$OMP BARRIER !\$OMP MASTER call MPI_Xxx(...) !\$OMP END MASTER !\$OMP BARRIER #pragma omp barrier
#pragma omp master
MPI_Xxx(...);
#pragma omp barrier

There are no synchronizations with "omp master", thus needs a barrier before and after, to ensure that data and buffers are available before and/or after MPI calls



MPI_THREAD_SERIALIZED

Only one thread at a time will make calls to the MPI library, but all threads are eligible to make such calls as long as they do not do so at the same time.



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MPI_THREAD_SERIALIZED



- MPI calls:
- Outside the parallel region
- Inside the parallel region with "omp single"

!\$OMP BARRIER !\$OMP SINGLE call MPI_Xxx(...) !\$OMP END SINGLE

#pragma omp barrier
#pragma omp single
 MPI_Xxx(...);

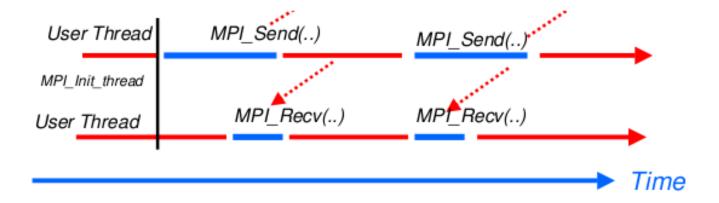
OMP_BARRIER is needed since OMP_SINGLE only guarantees synchronization at the end



MPI_THREAD_MULTIPLE

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 Each thread can make communications at any times. Less restrictive and very flexible, but the application becomes very hard to manage



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THREAD FUNNELED/SERIALIZED vs. Pure MPI

FUNNELED/SERIALIZED:

- All other threads are sleeping while just one thread is communicating.
- Only one thread may not be able to lead up max internode bandwidth
- Pure MPI:
 - Each CPU communication can lead up max internode bandwidth
- Hints: Overlap communications and computations.



Overlap comunications and computations

- Need at least MPI_THREAD_FUNNELED.
- While the master or the single thread is making MPI calls, other threads are doing computations.
- It's difficult to separate code that can run before or after the exchanged data are available

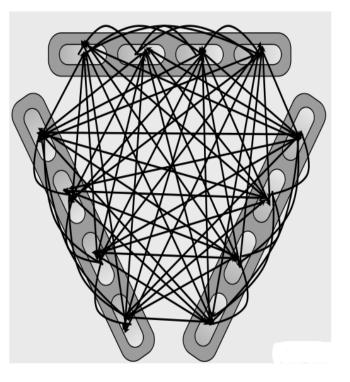
!SOMP PARALLEL if (thread id==0) then call MPI_xxx(...) else do some computation endif **!SOMP END PARALLEL**





MPI collective hybridization

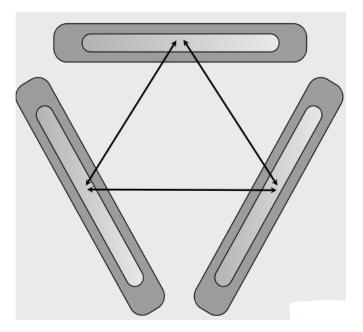
- MPI collectives are highly optimized
- Several point-to-point communication in one operations
- They can hide from the programmer a huge volume of transfer (MPI_Alltoall generates almost 1 million point-to-point messages using 1024 cores)
- There is no non-blocking (no longer the case in MPI 3.0)





MPI collective hybridization

- Hybrid implementation:
- Better scalability by a reduction of both the number of MPI messages and the number of process. Tipically:
- for all-to-all communications, the number of transfers decrease by a factor #threads^2
- the length of messages increases by a factor #threads
- Allow to overlap communication and computation.

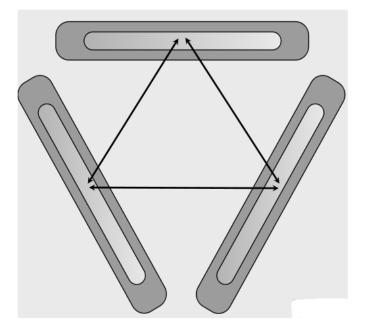






MPI collective hybridization

- Restrictions:
- In MPI_THREAD_MULTIPLE mode is forbidden at any given time two threads each do a collective call on the same communicator (MPI_COMM_WORLD)
- 2 threads calling each a MPI_Allreduce may produce wrong results
- Use different communicators for each collective call
- Do collective calls only on 1 thread per process(MPI_THREAD_SERIALIZED mode should be fine)



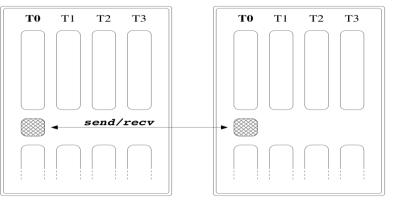


Hybrid programming via Multithreaded library

- Introduction of OpenMP into existing MPI codes includes OpenMP drawbacks (synchronization, overhead, quality of compiler and runtime...)
- A good choice (whenever possible) is to include into the MPI code a multithreaded, optimized library suitable for the application.
- BLAS, LAPACK, NAG (vendor), FFTW are well known multithreaded libraries available in the HPC arena.
- MPI_THREAD_FUNNELED (almost) must be supported.



Hybrid programming via Multithreaded library



SMP NODE

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SMP NODE

Only the master thread can do MPI communications (Pseudo QE code)

begin OpenMP region do i = 1, nsl in parallel call 1D-FFT along z (f[offset]) end do

```
# end OpenMP region
```

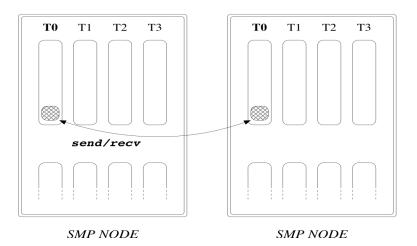
call fw_scatter(...)

```
# end OpenMP region
```

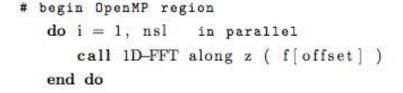
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Hybrid programming via Multithreaded library



Funneled: master thread do MPI communications within parallel region (Pseudo QE code)



```
# begin of OpenMP MASTER section
call fw_scatter( ... )
# end of OpenMP MASTER section
# force synchronization with OpenMP barrier
```

```
do i = 1, nzl in parallel
   do j = 1, Nx
        if ( dofft[j] ) then
            call 1D-FFT along y ( f[offset] )
        end do
        call 1D-FFT along x ( f[offset] ) Ny-times
   end do
# end OpenMP region
```



Hybrid programming via Domain decomposition

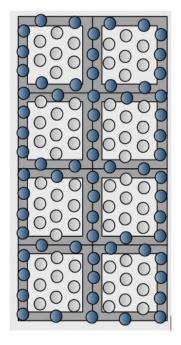
- Starting point is a well known MPI parallel code that solve Helmoltz Partial Differential Equation on a square domain.
- Standard domain decomposition (into slices for simplicity).
- No huge I/O
- The benchmark collect the timing of the main computational routine (Jacobi), GFLOPS rate, the number of iterations to reach fixed error and the error with respect to known analytical solution



Domain decomposition

 In the MPI basic implementation, each process has to exchange ghost-cells at every iteration (also on the same node)

```
regcnt = 0
     if (me.ne. 0) then
         receive stripe mlo from left neighbour blocking
!
       reacnt = reacnt + 1
        call MPI_IRECV( uold(1,mlo), n, MPI_DOUBLE_PRECISION, me,1, 11,
MPI_COMM_WORLD,reqary(reqcnt),ierr)
     end if
     if (me.ne. np-1) then
         receive stripe mhi from right neighbour blocking
       reacnt = reacnt + 1
...
     if (me.ne. 0) then
         send stripe mlo+1 to left neighbour async
reacnt = reacnt + 1
        call MPI_ISEND ( u(1,mlo+1), n, MPI_DOUBLE_PRECISION,
           me-1, 12, MPI_COMM_WORLD, regary(regcnt), ierr)
end if
```







Domain decomposition

The pseudo code for the rest of the Jacobi routines:

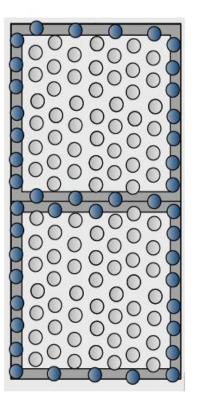
```
do j=mlo+1,mhi-1
do i=1,n
uold(i,j) = u(i,j)
enddo
enddo
call MPI_WAITALL ( reqcnt, reqary, reqstat, ierr)
```





Domain decomposition hybridization

- The hybrid approach allows you to share the memory area where ghost-cells are stored
- In the Hybrid Masteronly, each thread has not to do MPI communication within the node, since it already has available data (via shared memory).
- Communication decreases as the number of MPI process, but increases MPI message size for Jacobi routine.





Hybrid Masteronly Domain decomposition

Advantages:
 No message passing inside SMP nodes
 Simplest hybrid parallelization (easy to implement)
 Major problems:

-- All other threads are sleeping while master thread communicate



MPI_THREAD_FUNNELED Domain decomposition

Only the master	
thread can do MPI	!\$omp parallel_default(shared)
communications.	!\$omp master
communications.	error = 0.0
	if (me .ne. 0) then
	! receive stripe mlo from left neighbour blocking
	reqcnt = reqcnt + 1
	call MPI_IRECV(uold(1,mlo), n, MPI_DOUBLE_PRECISION, &
The other threads are	د me-1, 11, MPI_COMM_WORLD, reqary(reqcnt), ierr)
sleeping as in the	end if
previous case	
previous cuse	!\$omp end master
	!\$omp.do
	do j=mlo+1,mhi-1 do i=1,n
	uold(i,j) = u(i,j)
	enddo
	enddo
	!\$omp end do
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MPI_THREAD_FUNNELED Domain decomposition

	!
The barrier is needed	!!
after omp_ master	
directive in order to	
ensure correctness of	e
results.	

```
!$omp master
call MPI_WAITALL (regcnt, regary, regstat, ierr)
!$omp end master
!$omp barrier
 Compute stencil, residual, & update
 $omp do private(resid) reduction(+:error)
     do j = mlo+1, mhi-1
       do i = 2, n-1
           ....
 error = error + resid*resid
       end do
     enddo
!$omp end do
!$omp master
     call MPI ALLREDUCE (error local, error, 1, &
        MPI_DOUBLE_PRECISION, MPI_SUM, MPI_COMM_WORLD, ierr)
   £
!$omp end master
!$omp end parallel
```



MPI_THREAD_SERIALIZED Domain decomposition

<u>omp_single</u> guarantee serialized threads access . Note that no barrier is needed because omp_single guarantee synchronization at the end	<pre>!\$omp parallel default(shared) !\$omp single error = 0.0 reqcnt = 0 if (me .ne. 0) then ! receive stripe mlo from left neighbour blocking reqcnt = reqcnt + 1 call MPI_IRECV(uold(1,mlo), n, MPI_DOUBLE_PRECISION, & me-1, 11, MPI_COMM_WORLD,reqary(reqcnt),ierr) end if !\$omp end single if (me .ne. np-1) then ! receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking reqcnt = reqcnt + 1 call MPI_IBECV(uold(1 mbi), n, MPI_DOUBLE_PRECISION, & receive stripe mhi from right neighbour blocking</pre>
	reqcnt = reqcnt + 1 call MPI_IRECV(uold(1,mhi), n, MPI_DOUBLE_PRECISION, & & me+1, 12, MPI_COMM_WORLD, reqary(reqcnt), ierr) end if !\$omp end single
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MPI_THREAD_SERIALIZED Domain decomposition

omp_single guarantee only one threads access to the MPI_Allreduce collective.

```
!$omp do private(resid) reduction(+:error)
      do j = mlo+1, mhi-1
        do i = 2,n-1
    Evaluate residual
          resid = (ax^*(uold(i-1,j) + uold(i+1,j)) &
   £
                + ay^{*}(uold(i, j-1) + uold(i, j+1)) \&
   Æ
                + b * uold(i,j) - f(i,j))/b
! Update solution
          u(i,j) = uold(i,j) - omega * resid
! Accumulate residual error
          error = error + resid*resid
        end do
      enddo
!Somp end do
!$omp single
      error local = error
      call MPI ALLREDUCE (error local, error, 1, ...)
!$omp end single
!Somp end parallel
```



MPI_THREAD_MULTIPLE Domain decomposition

- Each thread can make communications at any times (in principle)
- ✤ Some little change in the Jacobi routine
- Use of *omp sections* construct (it ensures that each thread is allowed a different MPI call at the same time)
- Use of omp single for MPI_Waitall and collectives

MPI_THREAD_MULTIPLE

leftr, rightr,lefts and rights must to be private to ensure correct MPI calls.	<pre>!\$omp parallel default(shared) private(leftr,rightr,lefts,rights) error = 0.0 !\$omp sections !\$omp section if (me .ne. 0) then ! receive stripe mlo from left neighbour blocking leftr=me-1 else leftr=MPI_PROC_NULL endif call MPI_IRECV(uold(1,mlo), n, MPI_DOUBLE_PRECISION, & & leftr, 11, MPI_COMM_WORLD,reqary(1),ierr) !\$omp section</pre>
CINECA	<pre>!\$omp end sections !\$omp do do j=mlo+1,mhi-1 do i=1,n uold(i,j) = u(i,j) enddo enddo enddo enddo !\$omp end do</pre>

MPI_THREAD_MULTIPLE

omp single is used both for MPI_Waitall call that for MPI_Allreduce collective.

```
is used! Evaluate residual<br/>resid = (ax*(uold(i-1,j) + uold(i+1,j)) ...<br/>...PI_Waitall...<br/>...or! Update solution
```

```
....
! Update solution
u(i,j) = uold(i,j) - omega * resid
! Accumulate residual error
```

```
error = error + resid*resid
```

```
...
!$omp end do
!$omp single
```

```
..
```

```
call MPI_ALLREDUCE ( error_local, error,1,...)
error = sqrt(error)/dble(n*m)
!$omp end single
!$omp end parallel
```



Some results on FERMI@CINECA

Up to 64 hardware threads per process			
are available on bgq (SMT)	Number of threads (process for MPI only) per node	MPI+OpenMP (64 MPI, 1 process per node) MPI_THREAD_MULTIPLE version Elapsed time (sec.)	MPI (1024 MPI, 16,32,64 processes per node) Elapsed time (sec.)
Huge simulation, 30000x30000 points. Stopped after 100 iterations only for timing purposes.	1	78.84	N.A
	4	19.89	N.A
	8	10.33	N.A
	16	5.65	5.98
	32	3.39	7.12
CINECA	64	2.70	12.07

Cache-friendly Hybrid programming

- Modern CPUs continues to evolve....
- progressively higher cores count
 - The problem: memory bandwidth is increasing a lower rate than FLOPs

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- Solution: modern architectures feature large on-die caches of O(10) MB to increase overall performances
- Take advantage of caches involves data reuse...
- Take advantage of multicore and cluster of multicores involve hybridization
- Standard hybrid programming disadvantages:
- messages are larger
- cache is not shared among all threads within a node
- The solution: cache-friendly hybrid programming



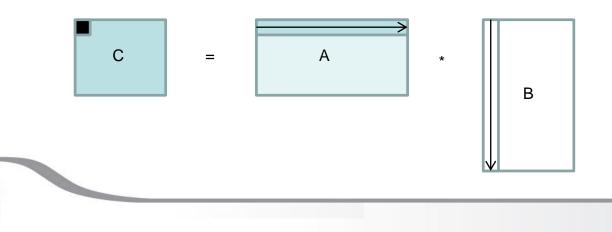


Case study: Matrix Multiply

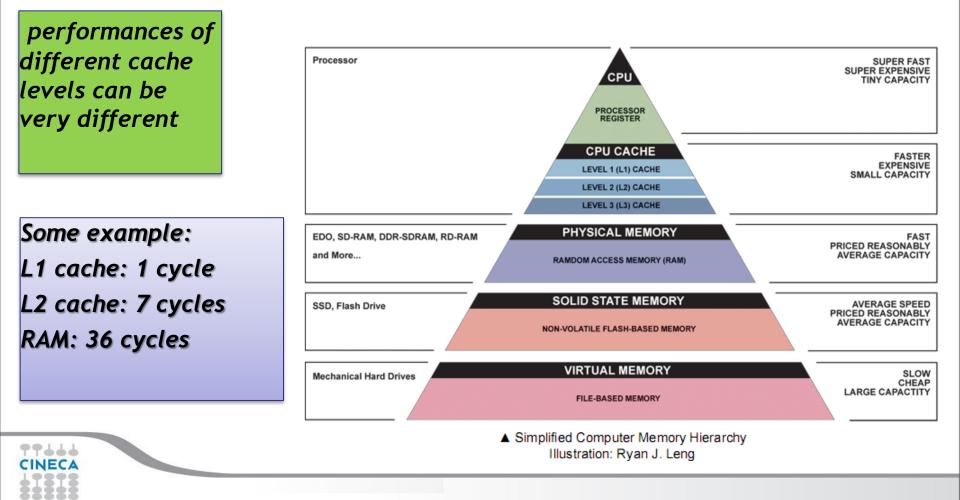
do i = ioff, iend do j = joff, jend do l = loff, lend c(i, j) = c(i, j) + a(i, l) * b(l, j) end do end do end do

Serial - textbook algorithm

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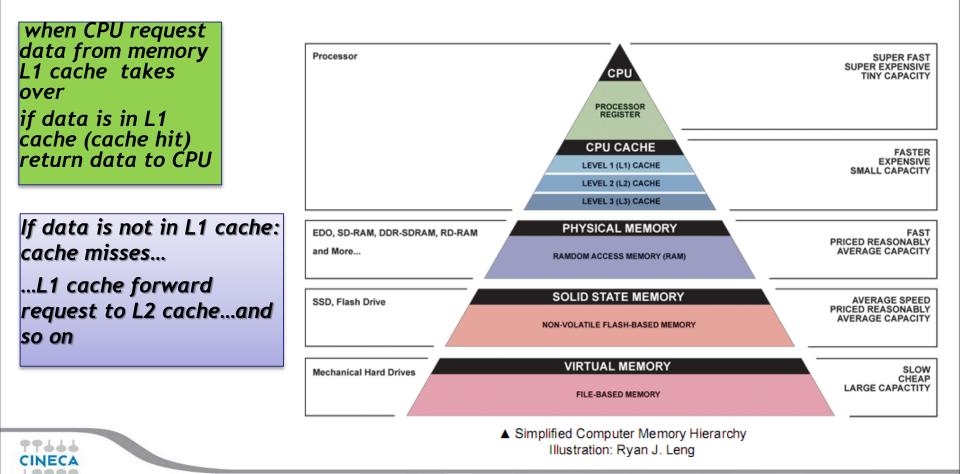


The memory hierarchy





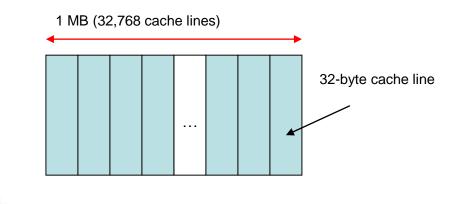
The memory hierarchy again





Cache effects on performance

- Cache miss degrading performances
- Increasing cache hit rate _____ higher performances
- Efficiency directly related to the reuse of data in cache
- Cache is organized in cache lines....





Cache classification

- Direct-mapped cache
- Given a memory cache line it is placed in one specific cache line in cache
- Fully associative cache
- Given a memory cache line it can be placed in **any** of the cache line in cache

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- N-way set associative cache
- Given a memory cache line it can be placed in any of N cache lines in cache

Direct-mapped and (partially) N-way set associative caches may lead to cache thrashing

Cache thrashing

No cache reuse! Repeatedly displacing and

loading cache lines Poor performance!

i=0:

load line X[0]-X[3] into cache; load X[0] from cache to register; load line Y[0]-Y[3] into cache, displacing line X[0]-X[3]; load Y[0] from cache into register; add, update Y[0] in cache; i=1: load X[0]-X[3] into cache, displacing Y[0]-Y[3], write line Y[0]-Y[3] back to memory; load X[1] from cache to register; load Y[0]-Y[3] into cache, displacing X[0]-X[3]; load Y[1] from cache to register; add, update Y[1] in cache; i=2: load X[0]-X[3] into cache, displacing Y[0]-Y[3], write line Y[0]-Y[3] back to memory; load X[2] from cache to register; load Y[0]-Y[3] into cache, displacing X[0]-X[3];

load Y[2] from cache to register;

add, update Y[2] in cache;

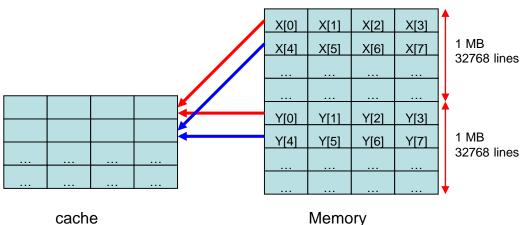
```
i=3: ...
```

double X[131072], Y[131072]; long i, j; // initialization of X, Y for(i=0:i<131072:i++) Y[i] = X[i] + Y[i];



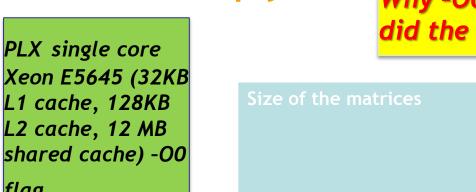
Assumptions:

- Direct-mapped cache
- Cache size: 1 MB;
- Cache line: 32 bytes;



Cache thrashing for matrix multiply

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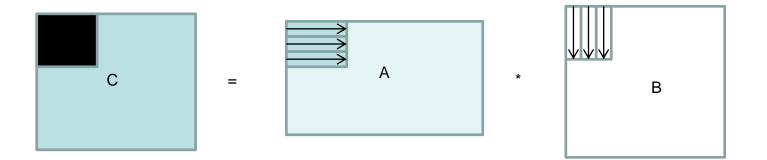


Why -OO? Otherwise the compiler did the right think with all codes

L1 cache, 128KB L2 cache, 12 MB shared cache) -OO flag	Size of the matrices	MFLOPs for the Matrix Multiply	MFLOPs/size
Degrading	128	119	0.92
performances due to	256	93	0.36
excessive cache	512	93	0.18
thrashing (size	1024	86	0.08
is a power of 2)	2048	61	0.02
	4096	33	0.008

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Great idea: blocking!

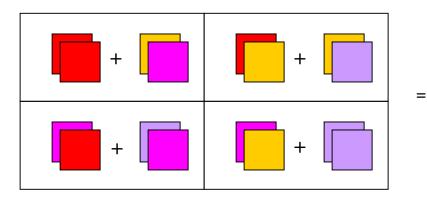


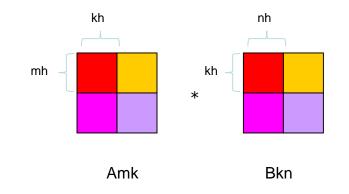
Better performances due to better cache reuse. Choose optimal blocking size is crucial.





Blocks matrix multiply: a simple example





Cmn

m, k, n: matrixes sizes

mh, kh, nh: block sizes, "Free" parameters

mb, kb, nb: number of blocks



Blocking algorithm

do ib = 0, mb-1

ioff = 1 + ib * mh

Loops over Matrix bloks

iend = MIN(m, ioff+mh-1) do jb = 0, nb-1 joff = 1 + jb * nhjend = MIN(n, joff+nh-1)do lb = 0, kb-1loff = 1 + lb * khlend = MIN(k, loff+kh-1) ! Cij = Aik * Bkj do i = ioff, iend do j = joff, jend do l = loff, lend c(i, j) = c(i, j) + a(i, l) * b(l, j)end do end do Loops inside end do end do Matrix block end do end do

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Blocking algorithm

PLX single core Xeon E5645 (32KB L1 cache, 128KB L2 cache, 12 MB shared cache) -O0 optimization flag, number of blocks fixed to 64 for simplicity **Better**

performances

but again not

good

Size of the matrices	MFLOPs for the Matrix Multiply	MFLOPs/size
128	97	0.75
256	120	0.46
512	124	0.24
1024	126	0.12
2048	122	0.05
4096	98	0.02



Matrix multiply OpenMP algorithm

```
!$omp parallel do default(none) &
!$omp shared(a,b,c,ioff,joff,loff,iend,jend,lend) &
!$omp private(i,j,l)
do i = ioff, iend
    do j = joff, jend
    do l = loff, lend
        c(i, j) = c(i, j) + a(i, l) * b(l, j)
        end do
    end do
end do
!$omp end parallel do
```

base version what about performances?





Matrix multiply OpenMP algorithm

PLX single core Xeon			
E5645 (32KB L1 cache, 128KB L2 cache, 12 MB shared cache)	Size of the matrices	MFLOPs for the Matrix Multiply (4 OpenMP threads)	MFLOPs/size
(-00 -openmp)			
	128	357	2.78
Better	256	373	1.45
performances but again not so	512	369	0.72
good	1024	337	0.32
	2048	225	0.10
77333	4096	109	0.02
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OpenMP blocking algorithm

```
!$omp parallel do default(none) &
!$omp
            shared(a,b,c,mb,nb,kb,m,n,k,mh,nh,kh) &
            private(ib,jb,lb,i,j,l,ioff,joff,loff,iend,jend,lend)
!$omp
 do ib = 0, mb-1
   ioff = 1 + ib * mh
   iend = MIN( m, ioff+mh-1)
   do jb = 0, nb-1
     joff = 1 + jb * nh
     jend = MIN( n, joff+nh-1 )
     do lb = 0, kb-1
       loff = 1 + lb * kh
       lend = MIN(k, loff+kh-1)
       ! Cij = Aik * Bkj
       do i = ioff, iend
         do j = joff, jend
           do l = loff, lend
             c(i, j) = c(i, j) + a(i, l) * b(l, j)
           end do
         end do
       end do
     end do
   end do
 end do
!$omp end parallel do
```

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OpenMP blocking algorithm

PLX single core Xeon E5645 (32KB L1 cache, 128KB L2 cache, 12 MB shared cache) -O0 -openmp flag number of blocks fixed to 64 for simplicity	Size of the matrices	MFLOPs for the Matrix Multiply (4 OpenMP threads)	MFLOPs/size
	128	268	2.09
Better scaling	256	477	1.86
with size and	512	494	0.96
better performances	1024	502	0.49
	2048	486	0.23
CINECA	4096	398	0.09

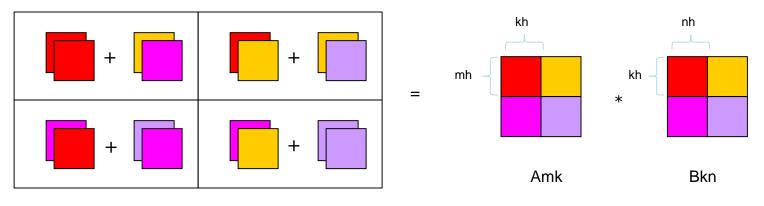
MPI+OpenMP blocking algorithm

- □ In general, a given matrix cannot be stored in a single node memory
- Matrix multiply takes too long (scale as a cubic power of matrix size)
- Target: increase the number of processors, mantaining local matrix size as constant as possible
- Use cache blocking algorithm within the single node
- MPI outside the node (simplest implementation)



Blocks again!

Assign blocks to tasks



Cmn

m, k, n: matrixes sizes

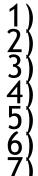
mh, kh, nh: block sizes, "Free" parameters

mb, kb, nb: number of blocks

Remark: I need to minimize communications



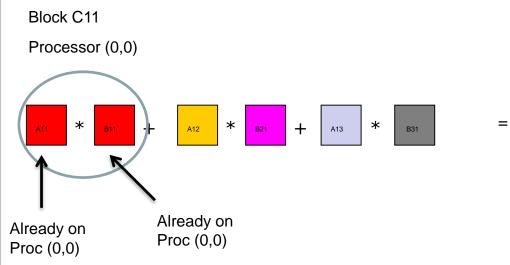
In details



Distribute processors on a 2D mesh (2D-Torus is good as well) Processor grid has dimension PxQ Each processor has his coordinates (p,q) Partition the matrixes into PxQ blocks Distribute blocks to processors Perform block by block operations, local to each processor Communicate blocks between processors Summer School on PARALLEL COMPUTING







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Consider 3x3 processor grid

AM	A12	A13	
A21	A22	A23	
A31	A32	A33	

4	B12	B13
B21	B22	B23
B31	B32	B33

Amk

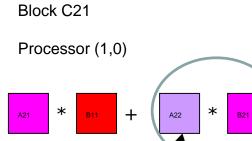
Bkn

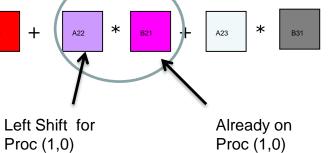
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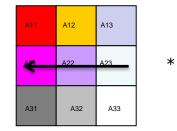


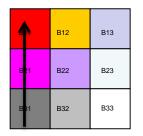
Consider 3x3 processor grid

=







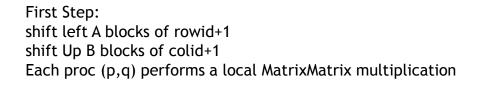


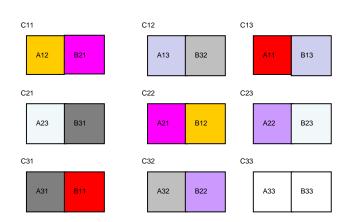
Amk

Bkn

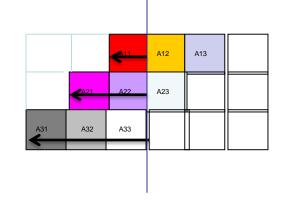


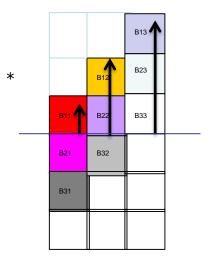






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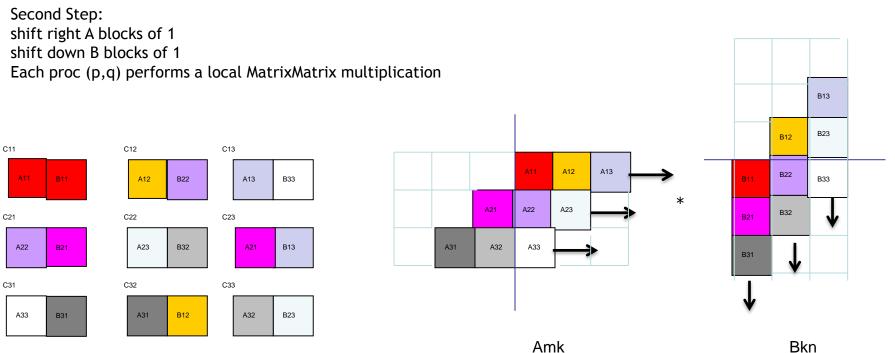


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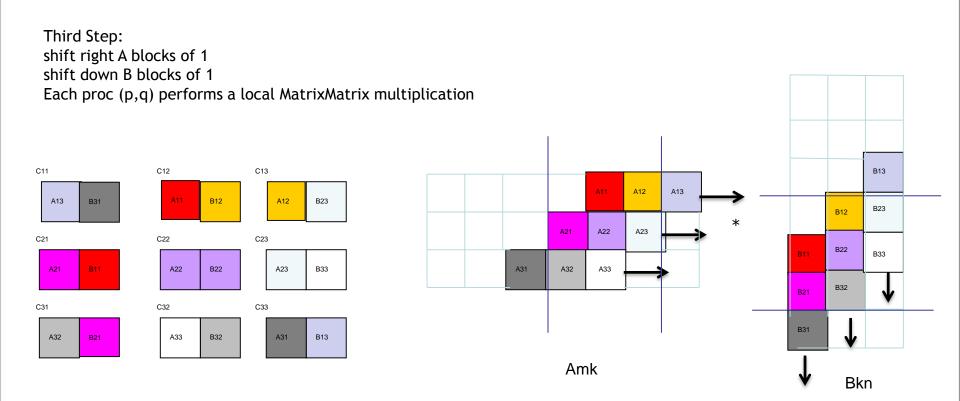


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Bkn









Hybrid MPI+OpenMP Cannon's scaling

PLX runs up to 64

cores, use standard

Blocking algorithm MPI_THREAD_FUNNELED for communication

optimization flags (- O) number of blocks fixed to 64 for simplicity	Size of t	ne matrices	MFLOPs for the MPI Cannon's Matrix Multiply	MFLOPs for the Hybrid Cannon's Matrix Multiply (4 OpenMP threads)
64 proc. case, Hybrid code is about 2.5 faster than MPI	2048	(1 MPI)	836	3315
	4096	(4 MPI)	3303	8366
	8192	(16 MPI)	13104	50246
	16384	(64 MPI)	51343	121230

Blocking algorithm Hybrid code is faster than simple MPI+OpenMP code

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Hybrid MPI+OpenMP Cannon's scaling

Blocking algorithm MPI_THREAD_FUNNELED for communication

optimization flags (- O) number of blocks fixed to optimal 128 Hybrid code is	Size of the matrices		MFLOPs for the MPI Cannon's Matrix Multiply	MFLOPs for the Hybrid Cannon's Matrix Multiply (4 OpenMP threads)
about 3.5	2048	(1 MPI)	1063	3882
faster than MPI	4096	(4 MPI)	4266	15083
	8192	(16 MPI)	16366	55215
	16384	(64 MPI)	64284	216781
Blog	king al	aorithm Hyb	rid code is faster	than simple



PLX runs up to 64

cores, use standard

Blocking algorithm Hybrid code is faster than simple MPI+OpenMP code

Lesson learned I

- Better scalability by a reduction of both the number of MPI messages and the number of processes involved in collective communications and by a better load balancing.
- Better adeguacy to the architecture of modern supercomputers while MPI is only a flat approach.
- Optimization of the total memory consumption (through the OpenMP sharedmemory approach, savings in replicated data in the MPI processes and in the used memory by the MPI library itself).
- Reduction of the footprint memory when the size of some data structures depends directly on the number of MPI processes.
- It can remove algorithmic limitations (maximum decomposition in one direction for example).

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Applications that can benefit from Hybrid programming

- Codes having limited MPI scalability (through the use of MPI_Alltoall for example).
- Codes requiring dynamic load balancing
- Codes limited by memory size and having many replicated data between MPI processes or having data structures that depends on the number of processes.
- Inefficient MPI implementation library for intra-node communication.
- Codes working on problems of fine-grained parallelism or on a mixture of fine and coarse-grain parallelism.
- Codes limited by the scalability of their algorithms.



Lesson learned II

- Achieving high-performance on modern CPUs requires algorithm which take full advantage of its computing resources and memory hierarchy.
- Using blocking and other cache-friendly techniques may help in writing efficient, hybrid-parallel applications, suitable for present and future computer architectures.

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Conclusions: there is no golden rule....

- Hybrid programming is complex and requires high level of expertise.
- Both MPI and OpenMP performances are needed (Amdhal's law apply separately to the two approaches).
- Savings in performances are not guaranteed (extra additional costs).





- Carlo Cavazzoni for Cache Friendly Hybrid Programming part
- Luca Ferraro and Francesco Salvadore for Hybrid Programming exercises part
- All CINECA SCAI staff for useful discussions and suggestions