# Introduction to Molecular Simulations 

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## Outlook

1.Classic Molecular Dynamics
2.Focus on Biomolecules: data insights
3.Setting up a simulation: details and outputs
4.Analysis of data

## MD ingredients



## Coordinates

Data formats for Molecular simulations

Mostly used in classical MD:

- PDB format
- GROMOS format
- XPLOR
- XYZ
- DCD
- CRD PDB data


GROMOS data

| 31934 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1LEU | N | 1 | 5.263 | 7.019 | 4.949 |
| 1LEU | H1 | 2 | 5.337 | 7.054 | 5.010 |
| 1LEU | H2 | 3 | 5.213 | 6.951 | 5.005 |
| 1LEU | CA | 4 | 5.171 | 7.129 | 4.911 |
| 1LEU | CB | 5 | 5.114 | 7.193 | 5.038 |
| 1LEU | CG | 6 | 5.017 | 7.101 | 5.113 |
| 1LEU | CD1 | 7 | 4.995 | 7.155 | 5.255 |
| 1LEU | CD2 | 8 | 4.882 | 7.092 | 5.041 |
| 1LEU | C | 9 | 5.225 | 7.241 | 4.818 |
| 1LEU | $\bigcirc$ | 10 | 5.150 | 7.297 | 4.738 |
| 2GLN | N | 11 | 5.354 | 7.271 | 4.831 |
| 2GLN | H | 12 | 5.411 | 7.221 | 4.896 |
| 2GLN | CA | 13 | 5.422 | 7.376 | 4.751 |
| 2GLN | CB | 14 | 5.488 | 7.480 | 4.842 |
| 2GLN | CG | 15 | 5.391 | 7.555 | 4.935 |
| 2GLN | CD | 16 | 5.296 | 7.648 | 4.859 |
| 2GLN | OE1 | 17 | 5.334 | 7.722 | 4.769 |
| 2GLN | NE2 | 18 | 5.172 | 7.650 | 4.902 |
| 2GLN | HE21 | 19 | 5.143 | 7.595 | 4.983 |
| 2GLN | HE22 | 20 | 5.099 | 7.690 | 4.844 |
| 2GLN | C | 21 | 5.528 | 7.314 | 4.659 |
| 2GLN | $\bigcirc$ | 22 | 5.628 | 7.260 | 4.706 |

PPBEC

## 31934

generated by VMD

| N | 52.630001 | 70.190002 | 49.490002 |
| :--- | :--- | :--- | :--- |
| H1 | 53.369999 | 70.540001 | 50.099998 |
| H2 | 52.130001 | 69.510002 | 50.049999 |
| CA | 51.709999 | 71.290001 | 49.110001 |
| CB | 51.139999 | 71.930000 | 50.380001 |
| CG | 50.169998 | 71.010002 | 51.130001 |
| CD1 | 49.950001 | 71.550003 | 52.549999 |
| CD2 | 48.820000 | 70.919998 | 50.410000 |
| C | 52.250000 | 72.410004 | 48.180000 |
| O | 51.500000 | 72.970001 | 47.380001 |
| N | 53.540001 | 72.709999 | 48.310001 |
| H | 54.110001 | 72.209999 | 48.959999 |
| CA | 54.220001 | 73.760002 | 47.509998 |
| CB | 54.880001 | 74.800003 | 48.419998 |
| CG | 53.910000 | 75.550003 | 49.349998 |
| CD | 52.959999 | 76.480003 | 48.590000 |
| OE1 | 53.340000 | 77.220001 | 47.689999 |
| NE2 | 51.720001 | 76.500000 | 49.020000 |
| 1HE2 | 51.430000 | 75.949997 | 49.830002 |
| 2HE2 | 50.990002 | 76.900002 | 48.439999 |
| C | 55.279999 | 73.139999 | 46.590000 |
| O | 56.279999 | 72.599998 | 47.060001 |
| N | 54.990002 | 73.169998 | 45.290001 |
| H | 54.119999 | 73.540001 | 44.959999 |
| CA | 55.869999 | 72.620003 | 44.230000 |

## XYZ format

49.490002

099998
49.110001
50.380001
51.130001
52.549999
50.410000
47.380001
48.310001
8.959999
48.419998
49.349998
48.590000

99
49.830002
44.230000


## Timescale



- Protein Folding milliseconds/seconds (10-3-1s)
- Ligand Binding micro/milliseconds ( $10^{-6}-10^{-3} \mathrm{~s}$ )
- Enzyme catalysis micro/milliseconds ( $10^{-6}-10^{-3} \mathrm{~s}$ )
- Conformational transitions pico/nanoseconds ( $10^{-12}-10^{-9} \mathrm{~s}$ )
- Collective vibrations -
- 1 picosecond ( $10^{-12} \mathrm{~s}$ )
- Bond vibrations -
- 1 femtosecond ( $10^{-15} \mathrm{~s}$ )


## Equation of motion

The equations that describe the temporal evolution of a physical system is called equation of motion. There are different equations of motions, which characterize the motion with different levels of approximation:
, Time-dependent Schrödinger's Equation

- for quantum-mechanical system
> Newton's Equation
» for classical-mechanical system
> Langevin's Equation
- for stochastic system


## Force field

$$
\begin{aligned}
& V\left(\mathbf{r}_{1}, \mathbf{r}_{2}, \ldots, \mathbf{r}_{n}\right)=\sum_{\text {bond }} \frac{1}{2} k_{b_{n}}\left(b_{n}-b_{0 n}\right)^{2}+\sum_{\text {angle }}^{2} \frac{1}{2} k_{\theta_{n}}\left(\theta_{n}-\theta_{0 n}\right)^{2}+ \\
& +\sum_{\begin{array}{c}
\text { improper } \\
\text { dihedral }
\end{array}} \frac{1}{2} k_{\xi_{n}}\left(\xi_{n}-\xi_{0 n}\right)^{2}+\sum_{\text {dihedral }} k_{\phi_{n}}\left[1+\cos \left(m_{n} \phi_{n}-\delta_{n}\right)\right]+ \\
& +\sum_{\begin{array}{c}
\text { nonbonded } \\
\text { pairs }(i j)
\end{array}} \frac{C_{i j}^{(12)}}{r_{i j}^{12}}-\frac{C_{i j}^{(6)}}{r_{i j}^{6}}+\frac{1}{4 \pi \varepsilon_{0}} \frac{q_{i} q_{j}}{\varepsilon_{r} r_{i j}}
\end{aligned}
$$

The potential energy function, together with the parameters required to describe the behavior of different kinds of atoms and bonds ( $\mathrm{k}_{\mathrm{b}}, \mathrm{k}_{\theta}, \mathrm{k}_{\xi}, \mathrm{C}_{\mathrm{i}}$, ...), is called: force field.

Several force fields are currently used and the choice depends from the studied system. Some force field are better suited for nucleic acids, for example, while others for membrane proteins

## MD set up



[1] Ress PDA : Structurw Explorer:

FSS $c$ - Coople
t

A Mumuk or The EPIDB MyPDB: Login I Register An Information Portal to Biological Macromolecular Structures As of Tuesday May 12,2009 这 there are 57558 Structures (i) | PDB Statistice (3)

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## 2 rgr (2)

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Pod - Deivert Lrforration
Tilie
Shaker family voltage dependent potassium channel (kv1.2-kv2.1 paddle chimera channel) in association with beta subunit

Authors
Primary Citation

Lono, 5. E, Tao, X, Camptoll, EA. MacKInnon, ㅁ. (7007) Atomio sarusture of a voltape-dependentK+ channel in a lipid membranelike envirmiment Naturo 450:376-382
[Abstract] Publmea
Deposisoe 2007-09-13 Release 2007-11-20 LantModining (REVDAT) 2009-02-24

| Experimental Method | TYpe X-RAY DIFFRACTION Datu [EDS] |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Paramoters | $\begin{aligned} & \text { Rosolition }\|A\| \\ & 2.40 \\ & 2 \end{aligned}$ | - <br> 0.21 | $\begin{aligned} & \text { Lun } \\ & 2 \text { (obs.) } \end{aligned}$ | $\begin{aligned} & \text { R.Fren } \\ & 0.244 \end{aligned}$ |  | $\begin{aligned} & \text { Spoce Gry } \\ & \mathrm{P} 42,2 \end{aligned}$ |  |
| Unit Cell | Letegth $\left\{\begin{array}{l}\text { A }\end{array}\right.$ <br> Angles [7] | a mipht | $\begin{aligned} & 144.06 \\ & 90,00 \end{aligned}$ | B Buta | 144.05 90.00 | c gamma | $\begin{aligned} & 284,40 \\ & 90.00 \end{aligned}$ |

Images and visuallration
(ce) Biological Molecule 1 (>>


Display Options (1)
Jthol
King
WobMol
Mat SimpleViewer-
Mat Proterin Workshap QuickFDa
All tmages

- Capable of Japlayng biobpcel nolecuien.
http://www.rcsb.org/pdb


## Initial coordinates: X-Ray vs. NMR



Higher X-ray resolution allows to use a more reliable starting structure in terms of amino-acids stereochemistry and accuracy of atomic positions

Error on initial position of protein atoms determines local structural alterations of the protein structure

X-ray resolutions smaller than $2 \AA$ are much more reliable, although difficult to achieve. Generally, a resolution in the range $2<\mathrm{R}<3 \AA$ are acceptable. Beyond $3 \AA$ the uncertainty of the initial position may cause artefacts in the MD simulation

## Initial coordinates: X-Ray vs. NMR



NMR determined structure provide information in a more realistic physiological environment as compared to X-ray determined structures although this could result in lower quality of initial coordinates and incertainties in the position of atomic coordinates.

KcsA Potassium channel (PDB code: 2K1E)

## Workflow for running MD simulations in GROMACS



## PCA: how it works



Let's assume our simulation is definve by the vector Rn, that simply consists of the set of cartesian coordinates of Ca atoms at a given time step.

Question: what is the unity vector so that projection of $\mathbf{R}_{\mathrm{h}}$ on vector $\mathbf{v}$ is the largest possible?

Answer: it is the vector $\mathbf{v}$, so that the variance of the projected point $p$ of Rn onto $v$ is the largest possible
$p$ is the projection of vector $\mathbf{R}_{h}$ onto unity vector $\mathbf{v}$ (dot product between $\mathbf{v}$ and $\mathbf{R}_{h}$ )

## Eigenvalue equation

The average of projected points onto $\mathbf{v}$ is:

$$
\mu(v)=\langle v, \bar{x}\rangle
$$



Eigenvectors

Variance of projected point onto $\mathbf{v}$ is:

$$
\sigma^{2}(v)=\langle C v, v\rangle
$$

Variance of projected points along vector $\boldsymbol{v}$ can be expressed in terms of dot product between $v$ and $C v$.

## Essential Dynamics of Proteins



Eigenvalues are sorted in descending order: the first one corresponds to the maximum variance of the projected points. The corresponding eigenvectors are the best principal components of associated eigenvalues.

# Data visualizzation for Molecular Simulations 



## Molecular Dynamics Simulations

Did we reach equilibrium...?
$\mathrm{RMSD}=\sqrt{\frac{1}{N} \sum_{i=1}^{N}\left(r_{i}-r_{0}\right)^{2}}$

We need to make sure that all the chemical and physical properties of the system have reached an equilibrium, where their averages do not longer change as a function of time. A simple way to test this is by measuring the RMSD (root mean square deviation) of $\mathrm{C} \alpha$ carbon atoms position with respect to start.


PRACE

$$
\text { RMSF }=\sqrt{\frac{1}{N} \sum_{i=1}^{N}\left(r_{i}-\langle r\rangle\right)^{2}}
$$



RMSF is a simple tool to measure the rigidity of the polypeptide chain. It calculates the deviations of C-alpha atoms coordinates from their average position. The flexibility pattern reflects the location of secondary structure elements in the protein structure.


## g_anaeig: the flag -filt




## M2 helix KirBac 1.1 <br> first eigenvector

Visualizzation of trajectories


Tube representation of a filtered trajectory onto the first and second eigenvectors of the atomic fluctuation covariance matrix of porin OmpA

Picture produced with RasMol

g_anaeig: output of flag -proj

By default, 8 eigenvectors are considered for output using g_anaeig. This option can be set by using the flags -first and -end
g_anaeig -f trajectory.xtc -v eigenvec.trr -eig eigenval.xvg -s reference.gro -proj proj.xvg -first 1 -last 5

Graphic representation of classic MD simulations



1
0.75
0.5
0.25
$-0.25$
$-0.5$
$-0.75$
-1

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