An introduction to Python

Object-oriented programming Iteration Generators



Object-oriented programming

data+code->objects

- 00P/00D
- Classes
- Inheritance

Procedural programming

In traditional procedural programming, there are

- data
- functions working on data

>>> m1 = create_matrix(10, 20)

```
>>> fill_matrix(m1, 2.3)
```

```
>>> write_matrix(m1, "m1.raw")
```

Object-oriented programming

In object-oriented programming, data and functions working on data are tied on the same class:

```
>>> m1 = Matrix(10, 20)
```

```
>>> m1.fill(2.3)
```

```
>>> m1.tofile("m1.raw")
```

Classes

In object-oriented languages, every object is an instance of a particular class.

The class completely defines the object's type, so we'll refer indifferently to the object's type or to the object's class.

A class do not simply define the object's content: it defines also the objects *algebra*, i.e. all the operation supported by objects.

Design: interface and implementation

In (object-oriented) design it's a good idea to fix first the interface and then the implementation.

Remember:

Code to an interface, not to an implementation.

The Fraction class

We want to design and implement a Fraction class for fractions.

This is only for exercise: the standard library already has a fractions module implementing this class.

```
Expected interface:
    >>> fr = Fraction(2, 3)
     >>> print("{}/{}".format(fr.numerator, fr.denominator))
     2/3
Implementation:
     class Fraction(object):
         def __init__(self, numerator, denominator):
             self.numerator = numerator
             self.denominator = denominator
```

The __init__() method is the class initializer; it is called when the *Fraction* object is created.

The first argument is self, the instance to be initialized; this is the first argument for all the methods.

The initializer adds two attributes (numerator and denominator) to self.

Technically it's not a constructor, since the self object already exists.

The actual constructor is __new__() and is a special method (a class method). Normally there is no need to define it.

```
By default instance attributes are public:
    >>> f0 = Fraction(5, 2)
    >>> f0.numerator
     5
     >> f0.numerator = 7
     >>>
```

We now want to add a method that can be used to simplify the fraction.

The interface we want to implement is

```
>>> f0 = Fraction(15, 6)
```

```
>>> print("{}/{}".format(f0.numerator, f0.denominator))
```

15/6

```
>>> f0.simplify()
```

```
>>> print("{}/{}".format(f0.numerator, f0.denominator))
```

5/2

```
class Fraction(object):
    . . .
    def simplify(self):
        while True:
            for n in range(2, self.numerator - 1):
                if self.numerator % n == 0 and self.denominator % n == 0:
                    self.numerator //= n
                    self.denominator //= n
                    break
            else:
                break
```

It would be better to write simply

```
>>> print(f0)
```

instead of repeating the following code to print a fraction

```
>>> print("{}/{}".format(f0.numerator, f0.denominator))
```

All the Python objects can be converted to strings, so also our fractions can be printed; anyway, the default string conversion is not meaningful:

```
>>> print(f0)
```

<__main__.Fraction object at 0x7fc854692940>

```
>>>
```

What we would like to implement is the following interface:

```
>>> f0 = Fraction(15, 6)
```

```
>>> print(f0)
```

```
(15/6)
```

We need to define the __str__() method. It must return a string.

```
class Fraction(object):
         . . .
        def __str__(self):
            return "({}/{})".format(self.numerator, self.denominator)
Example:
    f0 = Fraction(15, 6)
    >>> print(f0)
    (15/6)
```

For the same reason, it would be better to change the default representation for fractions. It should be the Python source code that can be used to construct that object, so a good interface is:

```
>>> f0 = Fraction(15, 6)
```

```
>>> print(repr(f0))
```

```
Fraction(15, 6)
```

We need to define the __repr__() method. It must return a string.

```
class Fraction(object):
         . . .
        def __repr__(self):
             return "{t}({n}, {d})".format(
                t=type(self).__name__,
                 n=self.numerator, d=self.denominator)
Usage:
    >>> f0
    Fraction(15, 6)
```

Design: class invariants

A class invariant is a particular condition or property that the class instances must have. The entire public interface of the class must satisfy the class invariants.

In our case, we want that every fraction is always simplified.

Invariants are preserved only in the public interface: they are generally temporarily broken inside method.

We want to force that every Fraction object is automatically simplified:

```
>>> print(Fraction(15, 6))
```

(5/2)

We can force simplification during construction by calling the simplify method at the end of the initializer:

```
class Fraction(object):
    def __init__(self, numerator, denominator):
        ...
        self.simplify()
```

The invariant is broken if the public interface allows to obtain a fraction that is not simplified. Unfortunately this is possible, since we gave public access to the *numerator* and *denominator* attributes:

```
>>> f0 = Fraction(15, 6)
>>> f0
Fraction(5, 2)
>>> f0.numerator = 10
>>> f0
Fraction(10, 2)
```

Generally classes do not give public access to their *innards* (the *representation*); attributes are generally **private**. Helper functions can be added to give read-only access to the attributes.

Attributes whose name starts with a double underscore are **private**.

So we can change the implementation of the class by changing self.numerator with self.__numerator, and self.denominator wit self.__denominator.

Generally a single underscore is used. Attributes starting with underscore are considered **protected**.

```
class Fraction(object):
```

```
def __init__(self, numerator, denominator):
```

```
self.__numerator = numerator
```

```
self.__denominator = denominator
```

```
self.simplify()
```

def numerator(self):

```
return self.__numerator
```

As attributes, methods starting with double underscore are private, and methods starting with a single underscore are *considered* protected.

In this case, since the simplification is an invariant, the simplify method is useless in the public interface. It's better to avoid useless public functions or attributes, so we will protect this method.

We choose to have a protected, and not a private method, since using this method is useless, but not dangerous.

```
class Fraction(object):
    def __init__(self, numerator, denominator):
        ...
        self._simplify()
```

As an alternative, a read-only property can be used. A property is an attribute-like object: it is used as an attribute, but implemented as a member.

```
class Fraction(object):
```

• • •

@property

```
def numerator(self):
```

return self.__numerator

Properties are by default *read-only* attributes.

In this case, the public interface allows accessing numerator as a read-only member:

```
>>> f0.numerator
```

```
5
```

```
>>> f0.numerator = 10
```

Traceback (most recent call last):

File "<stdin>", line 1, in <module>

```
AttributeError: can't set attribute
```

>>>

Properties can be used not only to "protect" attributes, but also to create "virtual" attributes. For instance

```
>>> print(f0)
Fraction(5, 2)
>>> print(f0.value)
2.5
>>>
```

We can implement this interface without introducing a new attributes (depending on the other).

Properties can be used not only to "protect" attributes, but also to create "virtual" attributes. For instance

```
class Fraction(object):
```

```
. . .
```

```
@property
```

```
def value(self):
```

return self.__numerator / self.__denominator

Properties allow also the set operation. Consider this interface:

```
>>> f1 = Fraction(5, 6)
>>> print(f1)
(5/6)
>>> f1.numerator +=5
>>> print(f1)
(3/2)
```

Notice that the simplification invariant is satisfied after the numerator update. We can add a *property setter*.



@property

def numerator(self):

return self.__numerator

The property getter function is used in
read-only expressions such as:
>>> print(fr.numerator)

@numerator.setter

def numerator(self, value):

self.__numerator = value

self._simplify()

The property setter function is used in assignment expressions such as: >>> fr.numerator = 9

We will add a setter for the *numerator* and the *denominator* properties, but not for the *value*, since our interface does not need it.

Properties can also have a deleter, which is called when the property attribute is deleted, for instance:

```
>>> del obj.prop
```

If the property *prop* has deleter function, it is called; otherwise an error is raised.

In this case, we won't define a deleter, since our interface don't need it, and since it would be absurd to delete the numerator or the denominator.

We now want to add arithmetic to our class. The interface we want to implement is the simplest one:

```
>>> f0 = Fraction(5, 2)
>>> f1 = Fraction(2, 3)
>>> f0 + f1
Fraction(19, 6)
>>>
```

```
In order to allow addition, the __add__ method must be added:
```

```
class Fraction(object):
```

. . .

```
def __add__(self, other):
```

```
return Fraction(
```

numerator=self.numerator * other.denominator + \

other.numerator * self.denominator,

denominator=self.denominator * other.denominator)

The operator syntax is only *syntactic sugar*: indeed operators are simply methods with a special name. What we write is

>>> f0 + f1

but what the interpreter executes is

```
>>> f0.__add__(f1)
```

It would be nice to be able to mix fractions and integers in arithmetic expressions, as we can do with float and int objects:

```
>>> f0 = Fraction(5, 2)
>>> print(f0 + 5)
(15/2)
>>> print(5 + f0)
(15/2)
>>>
```

The first mixed expression (f0 + 5) can be obtained by slightly changing the method:

```
def __add__(self, other):
```

```
if not isinstance(other, Fraction):
```

```
other = Fraction(other, 1)
```

```
return Fraction(...)
```

The isinstance(other, Fraction) function returns True if other is a Fraction (introspection).

The second mixed expression (5 + f0) can be obtained by adding a __radd__ (reverse add) method.

```
Indeed, when an expression obj0 + obj1 is found, the interpreter first tries to execute it as obj0.\_add\_(obj1); if this is not possible, it then tries to execute obj1.\_radd\_(obj0).
```

In our case the implementation of the __radd__ method is simple, due to the commutative property of the addition:

```
def __radd__(self, other):
```

```
return self.__add__(other)
```

The Matrix class

We now want to design a Matrix class.

This is only an exercise: the numpy package contains a much better implementation.

We want to implement the following interface:

```
>>> m0 = Matrix(4, 10, fill=1.0)
>>> print(m0[2, 3])
1.0
>> m0[2, 3] = 5.5
>>> m1 = Matrix(4, 10, fill=2.0)
>>> m2 = m0 + m1
>>> m0 += m1
```

```
In order to implement the item access, as in
    >>> print(m0[2, 3])
we must implement the __getitem__(...) method:
    class Matrix(object):
         . . .
         def __getitem__(self, index):
             i, j = index
             return self.__data[i][j]
```

```
In order to implement the item assignment, as in
    >> m0[2, 3] = 5.5
we must implement the __setitem__(...) method:
    class Matrix(object):
         . . .
         def __setitem__(self, index, value):
             i, j = index
             self.__data[i][j] = value
```

We already know how to implement a class with the *add* interface. But notice the last line:

>>> m0 += m1

We know that, for immutable types, this += operation creates a new object; m0 becomes a symbolic name for that new object. Since a matrix can be very big, this is not memory efficient: it would be better to have a mutable type, and to change the matrix object *in-place*.

The __iadd__() method can be set to implement this in-place operator. It is defined as the __add__(); generally it returns the self object after it has been changed.

```
def __add__(self, other):
```

```
result = Matrix(self.__num_rows, self.__num_columns)
```

```
for i in range(self.__num_rows):
```

```
for j in range(self.__num_columns):
```

```
result[i, j] = self[i, j] + other[i, j]
```

return result

```
def __iadd__(self, other):
    for i in range(self.__num_rows):
        for j in range(self.__num_columns):
            self[i, j] += other[i, j]
        return self
```

Class attributes

Sometimes we need to set a class attribute, i.e. an attribute which is exactly the same for all the instances of the class.

In this case, it can be set directly in the class body.

For instance, in a Circle class we need to define the value of pi.

```
class Circle(object):
```

pi = 3.141592653589793

```
def __init__(self, radius):
```

self.radius = radius

```
def area(self):
```

```
return self.pi * self.radius ** 2
```

A class attribute belongs to the class, not to the instance. It can be accessed also through the class:

>>> print(Circle.pi)

3.141592653589793

>>>

Class methods

Sometimes we need to define a method whose behavior does not depend on the instance, but only on the class.

For instance, the Matrix class could implement a method to read the class from file. The file contains shape and data. The from_file method mustn't be applied to a constructed matrix, since a constructed matrix already has a shape (and data) that do not necessarily match the file content. It can be defined as class method.

The to_file(...) method is a normal instance method, which can be applied to an already constructed instance:

```
def to_file(self, filename):
```

```
with open(filename, "w") as f_out:
```

f_out.write("{!r} {!r}\n".format(

self.__num_rows, self.__num_columns))

for i in range(self.__num_rows):

for j in range(self.__num_columns):

f_out.write(str(self[i, j]) + '\n')

The matrix.from_file(...) method

```
@classmethod
def from_file(cls, filename):
    with open(filename, "r") as f_in:
        lst = f_in.readline().strip().split()
        num_rows, num_columns = int(lst[0]), int(lst[1])
        instance = cls(num_rows, num_columns)
        for i in range(num_rows):
            for j in range(num_columns):
                instance[i, j] = float(f_in.readline().strip())
    return instance
```

The first argument of an instance method is the instance itself; it is generally named self.

The first argument of a class method is the class itself; it is generally named cls.

Do not use other names!

```
>>> m = Matrix(2, 10, fill=2.5)
>>> m.to_file("m.txt")
>>> m2 = Matrix.from_file("m.txt")
>>> print(m2)
2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5
2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5 2.5
>>>
```

Other magic methods

The list of magic __methods__ is very long:

- __delitem__(): remove an item
- __len__(): return the object length
- __iter__(): iterate on the object
- __del__(): the finalizer; it's called just before the object is destroyed (normally there is no need to implement it)
- __call__(*args, **kwargs): if defined, the object can be called as a function (it's a *functor*).

Operators and magic methods

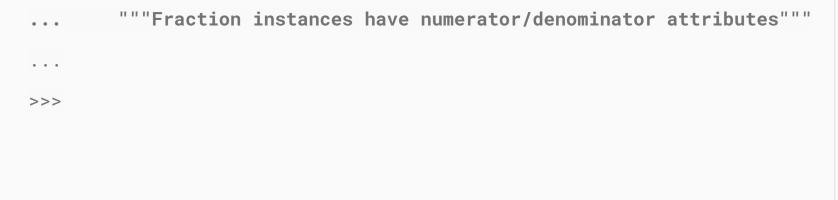
Almost all the Python operators have corresponding magic methods, so they can be defined in classes:

We can overwrite all this operators; anyway, we cannot change their precedence: the standard Python precedence will always be applied.

The class docstring

Also classes have docstrings.

```
>>> class Fraction(object):
```



Inheritance

Inheritance is an essential feature in object-oriented programming.

A class can inherit from another one (its *base class* or *superclass*). In this case, the derived class inherits all the content (attributes and methods) of its superclass.

We make use of inheritance to

- Change an existing behavior
- Add new behaviors
- Enforce a common (abstract) interface to a hierarchy of classes

We want to define a rstr class which behaves exactly as the builtin str, with the only exception that it is printed reversed:

```
>>> s = rstr("Hello, world!")
>>> print(s)
!dlrow ,olleH
>>>
```

A rstr is a str with a changed behavior.

Suppose we want to define a Path class to implement the path algebra:

```
>>> pdir = Path("/home/user/data")
```

```
>>> print(pdir)
```

/home/user/data

```
>>> print(pdir.dirname())
```

/home/user

```
>>> print(pdir.join("alpha", "beta", "gamma.txt"))
```

/home/user/data/alpha/beta/gamma.txt

A Path is a string with some more algebra. We can implement it by inheriting from the string class, and by defining the new behavior:

- Path.dirname()
- Path.basename()
- Path.split()
- Path.join(*args)
- . . .

We know that many dict-like types exist:

- dict
- defaultdict
- OrderedDict
- Counter

They all have a common interface. We will introduce a new frozendict class in the dictionary hierarchy.

The "is a" property

The inheritance relationship can be expressed as "is a":

- A rstr instance <u>is a</u> str
- A Path instance <u>is a</u> str
- A Counter instance is a Mapping

Changing an existing behavior: rstr

```
>>> class rstr(str):
... def __str__(self):
... return "".join(reversed(tuple(super().__str__())))
...
>>> s = rstr("Hello, world!")
>>> print(s)
!dlrow ,olleH
```

The base class is str, as stated in the first line. The __str__ method is replaced by a new one. Notice that its implementation calls the original method. Here super() represents the superclass, so super().__str__() is the original str method.

Class hierarchies

The "is a" property is maintained in complex hierarchies:

```
>>> class Animal(object): pass
```

```
>>> class Mammal(Animal): pass
```

```
>>> class Cat(Mammal): pass
```

```
>>> wasabi = Cat()
```

```
>>> isinstance(wasabi, Animal)
```

True

All the Python classes inherit (directly or indirectly) from object. This is the base of the entire class hierarchy.

Adding a new behavior: Path

```
class Path(str):
```

```
def dirname(self):
```

return Path(os.path.dirname(self))

```
def join(self, *parts):
    return Path(os.path.join(self, *parts))
...
```

The base class is str also in this case.

Here dirname() is a new method, while join() is an overriden method.

The frozendict hierarchy

```
from collections import Mapping
```

```
class frozendict(Mapping):
```

. . .

```
def __init__(self, *args, **kwargs):
```

```
self.__dct = dict(*args, **kwargs)
```

```
def __getitem__(self, key):
```

```
return self.__dct[key]
```

The base class is collections. Mapping. This is an abstract class enforcing the interface for an immutable mapping. When inheriting from this class, three methods must be defined:

- __getitem__
- __len__
- __iter__

Multiple inheritance

A class can have multiple base classes:

```
class Alpha(BaseA, BaseB, BaseC):
```

pass

Iteration

The glue between data and algorithms

• The iterable/iterator duality

Iterable/iterator

An *iterable* is an object allowing iteration on it. To iterate means to traverse the object's items, one item after the other.

An iterator is an object allowing iteration on an iterable.

- An object is *iterable* if its class has an __iter__() method returning an *iterator*.
- An object is an *iterator* if its class has a __next__() method returning the next iteration element.

```
The iter() function returns an iterator from an (iterable) object. It's a shorthand to call the object's __iter__() method.
```

```
>>> lst = [7, 11, 13]
```

```
>>> iterator = iter(lst)
```

```
>>> iterator
```

```
<list_iterator object at 0x7f5b56ebf9e8>
```

```
>>>
```

```
The next() function moves the iterator forward and returns the next item, if any. It's simply a shorthand to call the object's \_next\_() method.
```

```
>>> next(iterator)
7
>>> next(iterator)
11
>>> next(iterator)
13
>>>
```

Python 2 vs Python 3 The name of the *next* method

next()

__next__()

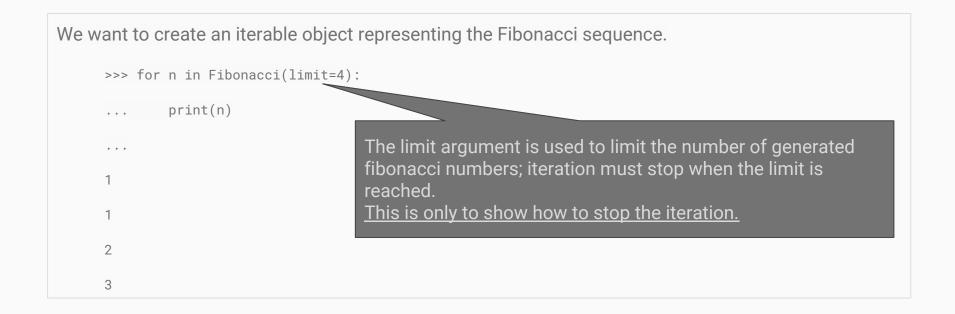
```
The iteration process stops when the __next__() method raises a StopIteration() exception.
    >>> next(iterator)
    Traceback (most recent call last):
        File "<stdin>", line 1, in <module>
        StopIteration
        >>>
```

We now understand how the for loop **for item in sequence** works:

- It creates an iterator to the sequence **iterator** = **iter(sequence)**
- It assigns item = next(iterator) (and then executes the loop's body) until next raises a StopIteration error



The Fibonacci iterable



The implementation of the Fibonacci class is quite simple:

```
class Fibonacci(object):
```

def __init__(self, limit=None):

self._limit = limit

def __iter__(self):

return Fibonaccilterator(self._limit)

We now need to implement the FibonacciIterator.

The FibonacciIterator initializer accepts the limit value and sets the internal iterator status:

```
class FibonacciIterator(object):
```

```
def __init__(self, limit):
```

```
self._limit = limit
```

```
self._count = 0
```

```
self._first, self._second = 1, 1
```

The status is needed to keep track of the current position in iteration and to save it between consecutive calls to the __next__ method.

The FibonacciIterator next method is responsible for

- Updating the internal status
- Returning the next iteration item
- Stopping the iteration when the limit is reached.

```
def __next__(self):
      self._count += 1
      if self._limit is not None and self._count > self._limit:
          raise StopIteration()
      if self._count <= 2:</pre>
          return 1
      else:
          self._first, self._second = self._second, self._first + self._second
          return self._second
```

The iteration process involves two classes and two objects, the *iterable* and the *iterator*. Is that necessary?

For instance, consider a Range class which emulates the builtin range function.

A naive implementation with a single class is possible.

```
A naive implementation with a single class:
```

```
class Range(object):
```

```
def __init__(self, stop):
```

```
self._stop = stop
```

```
self._index = 0
```

```
def __iter__(self):
    return self
```

```
def __next__(self):
    if self._index >= \
        self._stop:
        raise StopIteration()
    value = self. index
    self. index += 1
    return value
```

```
It seems to work:
```

```
>>> list(Range(6))
```

```
[0, 1, 2, 3, 4, 5]
```

```
>>>
```



```
class Range(object):
                                              class RangeIterator(object):
    def __init__(self, stop):
                                                 def __init__(self, stop):
        self._stop = stop
                                                     Self._stop, self._index = stop, 0
                                                 def __next__(self):
    def __iter__(self):
                                                     if self._index >= self._stop:
        return RangeIterator(self._stop)
                                                         raise StopIteration()
                                                     value = self._index
                                                     self._index += 1
                                                     return value
```

his works correctly, since two distinct iterators are used:
>>> for i in r:
for j in r:
<pre> print(i, j)</pre>
0 0
0 1
02
1 0
11

Generator functions

Creating iterable objects is not difficult, anyway we need to implement two cooperative classes. Luckily, Python supports a simpler way to implement iteration: generator functions (**generators**). A generator function is a function that can temporarily stop its execution, yield a value to the caller, and then be restarted by the caller; execution restarts just after the yield statement.

Generators use the yield statement instead of return.

The yield statement is a kind of "temporary" return: the execution of the function is suspended, and it's up to the caller to resume it.

When a generator is called, it returns an *iterator*; the caller then uses this iterator as usual. Any call to next restart the execution of the generator function.

When the generator function returns, a StopIteration is automatically raised.

```
Consider this function:
    >>> def range_gen(n):
    .... i = 0
        while i < n:
     . . .
        yield i
     . . .
        i += 1
     . . .
    . . .
    >>>
```

```
>>> r = range_gen(3)
>>> r
<generator object range_gen at 0x7f039be9b150>
>>> next(r)
0
>>> next(r)
1
```

```
>>> next(r)
2
>>> next(r)
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
StopIteration
>>>
```

Hands-on

Write a function that "returns" **all** the Fibonacci numbers, for instance to be used as follows:

>>> for n in fibonacci():

... if is_pandigital(n):
... print(n)
... break

def is_pandigital(n):

return len(set(str(n))) == 10

```
This is a solution:
    >>> def fibonacci(*, first=1, second=1):
     ... yield first
     ... yield second
           while True:
     . . .
                first, second = second, first + second
     . . .
         yield second
     . . .
     . . .
    >>>
```

Notice that the fibonacci() iterator never stops! It's up to the caller to stop the iteration. For instance:

```
>>> for index, n in zip(range(10), fibonacci()):
... print(index, n)
...
0 1
...
8 34
9 55
```

Generator expressions

Generator expressions have the list comprehension syntax with the generator semantics:

```
>>> [i ** 2 for i in range(5)]
```

```
[0, 1, 4, 9, 16]
```

```
>>> (i ** 2 for i in range(5))
```

<generator object <genexpr> at 0x7f06fc7181a8>

>>>

```
Suppose you want to sum all the squares of the first N integers:
    >>> sum([i ** 2 for i in range(10000)])
    333283335000
    >>> sum([i ** 2 for i in range(100000)])
    333328333350000
    >>> sum([i ** 2 for i in range(1000000)])
    333332833333500000
    >>>
```

This wastes a lot of memory: indeed this sum does not really need a container. Using generator expressions only one integer is in the memory at any time:

```
>>> sum((i ** 2 for i in range(100000)))
```

```
333332833333500000
```

>>>

When a generator expression is the only argument in a function call, parentheses can be omitted:

```
>>> sum(i ** 2 for i in range(100000))
```

```
333332833333500000
```

Modules

How to organize Python source

ModulesPackages

Python modules

A Python module is simply a Python source file with .py extension. Modules are libraries: they can be imported and used in other modules or programs.

```
(python3.5)$ cat greetings.py
```

```
def greet(who):
```

```
print("Hello, {}!".format(who))
```

```
def welcome(who):
```

```
print("Welcome, {}!".format(who))
```

Modules can be imported:

```
>>> import greetings
```

```
>>> dir(greetings)
```

```
['__builtins__', '__cached__', '__doc__', '__file__', '__loader__',
'__name__', '__package__', '__spec__', 'greet']
```

```
>>> greetings.greet("world")
```

Hello, world!

>>>

Specific symbolic names can be imported from a module:

```
>>> from greetings import greet, welcome
```

```
>>> greet("world")
```

```
Hello, world!
```

```
>>> welcome("Guido")
```

Welcome, Guido!

```
>>>
```

It is possible to import all the symbolic names from a module:

```
>>> from greetings import *
```

```
>>> greet("world")
```

```
Hello, world!
```

```
>>> welcome("Guido")
```

```
Welcome, Guido!
```

```
>>>
```

This is not a good idea, since it pollutes the namespace!

Generally modules contain an __all__ attribute, which is a list of the public symbolic names; when importing with *, only those names will be imported:

```
(python3.5)$ cat greetings.py
__all__ = [
    'greet',
    'welcome',
]
...
(python3.5)$
```

Module docstring

Modules have a docstring too; it's a function string at the beginning of the file

```
(python3.5)$ cat primes.py
```

```
"""Functions to test primality"""
```

```
def is_prime(n):
```

. . .

(python3.5)\$

Python packages

A Python package is a directory containing a module file __init__.py (the package initializer, which can be empty) and some other Python modules: for instance

```
number_theory/
```

```
__init__.py
```

primes.py

```
divisors.py
```

Packages can contain subpackages.

Hands-on

Organize the Fibonacci exercise in a module.

Create a package containing the Fibonacci module and the divisors module.