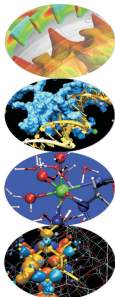


# Scientific and Technical Computing in C

Stefano Tagliaventi    Luca Ferraro

CINECA Roma - SCAI Department

Rome, 3-5 February 2016



## Arithmetic

- Integers
- Floating
- Expressions
- Mixing Types

## Aggregate

- Structures
- Defining Types
- Arrays
- Storage & C.
- More Arrays

- 1 Arithmetic Types and Math
  - Integer Types
  - Floating Types
  - Expressions
  - Arithmetic Conversions

- 2 Aggregate Types

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Computing == manipulating data and calculating results
  - Data are manipulated using internal, binary formats
  - Data are kept in memory locations and CPU registers
- C is quite liberal on internal data formats
  - Most CPU are similar but all have peculiarities
  - C only mandates what is *de facto* standard
  - Some details depend on the specific executing (a.k.a. target) hardware architecture and software implementation
  - C Standard Library provides facilities to translate between internal formats and human readable ones
- C allows programmers to:
  - think in terms of data types and named containers
  - disregard details on actual memory locations and data movements

# C is a Strongly Typed Language

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Each literal constant has a type
  - Dictates internal format of the data value
- Each variable has a type
  - Dictates content internal format and amount of memory
  - Type must be specified in a declaration before use
- Each expression has a type
  - And subexpressions have too
  - Depends on operators and their arguments
- Each function has a type
  - That is the type of the returned value
  - Specified in function declaration or definition
  - If the compiler doesn't know the type, it assumes `int`
- Function parameters have types
  - I.e. type of arguments to be passed in function calls
  - Specified in function declaration or definition
  - If the compiler doesn't know the types, it will accept any argument, applying some type conversion rules

# Integer Types (as on Most CPUs)

## Arithmetic

Integers  
 Floating  
 Expressions  
 Mixing Types

## Aggregate

Structures  
 Defining Types  
 Arrays  
 Storage & C.  
 More Arrays

Type	Sign	Conversion	Width (bits)		Size (bytes)	
			Minimum	Usual	Minimum	Usual
<b>signed char</b>	+/-	%hd <sup>1</sup>	8	8	1	1
<b>unsigned char</b>	+	%hu <sup>1</sup>				
<b>short</b>	+/-	%hd	16	16	2	2
<b>short int</b>						
<b>unsigned short</b>	+	%hu	16	32	2	4
<b>unsigned short int</b>						
<b>int</b>	+/-	%d	16	32	2	4
<b>unsigned</b>	+	%u				
<b>unsigned int</b>	+	%u	32	32 or 64	4	4 or 8
<b>long</b>	+/-	%ld				
<b>long int</b>	+/-	%ld	32	32 or 64	4	4 or 8
<b>unsigned long</b>	+	%lu				
<b>unsigned long int</b>	+	%lu	64	64	8	8
<b>long long<sup>2</sup></b>	+/-	%lld				
<b>long long int<sup>2</sup></b>	+/-	%lld	64	64	8	8
<b>unsigned long long<sup>2</sup></b>	+	%llu				
<b>unsigned long long int<sup>2</sup></b>	+	%llu				

Constraint: **short** width  $\leq$  **int** width  $\leq$  **long** width  $\leq$  **long long** width

1. C99, in C89 use conversion to/from **int** types
2. C99

- New platform/compiler? Always check with **sizeof (type)**
- Values of **char** and **short** types just use less memory, they are promoted to **int** types in calculations

# #include <limits.h>

## Arithmetic

Integers  
 Floating  
 Expressions  
 Mixing Types

## Aggregate

Structures  
 Defining Types  
 Arrays  
 Storage & C.  
 More Arrays

Name	Meaning	Value
<b>CHAR_BIT</b>	width of any <code>char</code> type	$\geq 8$
<b>SCHAR_MIN</b>	minimum value of <code>signed char</code>	$\leq -128$
<b>SCHAR_MAX</b>	maximum value of <code>signed char</code>	$\geq 127$
<b>UCHAR_MAX</b>	maximum value of <code>unsigned char</code> type	$\geq 255$
<b>SHRT_MIN</b>	minimum value of <code>short</code>	$\leq -32768$
<b>SHRT_MAX</b>	maximum value of <code>short</code>	$\geq 32767$
<b>USHRT_MAX</b>	maximum value of <code>unsigned short</code>	$\geq 65535$
<b>INT_MIN</b>	minimum value of <code>int</code>	$\leq -32768$
<b>INT_MAX</b>	maximum value of <code>int</code>	$\geq 32767$
<b>UINT_MAX</b>	maximum value of <code>unsigned</code>	$\geq 65535$
<b>LONG_MIN</b>	minimum value of <code>long</code>	$\leq -2147483648$
<b>LONG_MAX</b>	maximum value of <code>long</code>	$\geq 2147483647$
<b>ULONG_MAX</b>	maximum value of <code>unsigned long</code>	$\geq 4294967295$
<b>LLONG_MIN</b>	minimum value of <code>long long</code>	$\leq -9223372036854775808$
<b>LLONG_MAX</b>	maximum value of <code>long long</code>	$\geq 9223372036854775807$
<b>ULLONG_MAX</b>	maximum value of <code>unsigned long long</code>	$\geq 18446744073709551615$

- Use them to make code more portable across platforms
- New platform/compiler? Always check values

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Constants have types too
- Compilers must follow precise rules to assign types to integer constants
  - But they are complex
  - And differ among standards
- Rule of thumb:
  - write the number as is, if it is in `int` range
  - otherwise, use suffixes `U`, `L`, `UL`, `LL`, `ULL`
  - lowercase will do as well, but `1` is easy to misread as `l`
- Remember: do not write `spokes = bicycles*2*36;`
  - `#define SPOKES_PER_WHEEL 36`
  - or declare:  
`const int SpokesPerWheel = 36;`
  - and use them, code will be more readable, and you'll be ready for easy changes

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- `#include <stdlib.h>` to use:

Function	Returns
<code>abs ()</code>	absolute value of an <code>int</code>
<code>labs ()</code>	absolute value of a <code>long</code>
<code>llabs ()</code>	absolute value of a <code>long long</code>

- Use like: `a = abs (b+i) + c;`
- For values of type `short` or `char`, use `abs ()`



## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Integer types are encoded in binary format
  - Each one is a sequence of bits, each having state 0 or 1
  - Bitwise arithmetic manipulates state of each bit
- Each bit of the result of unary operator  $\sim$  is in the opposite state of the corresponding bit of the operand
- Each bit of the result of binary operators  $|$ ,  $\&$ , and  $\wedge$  is the OR, AND, and XOR respectively of the corresponding bits in the operands
- Precedence
  - $a\&b | c\wedge d\&e$  same as  $(a\&b) | (c\wedge(d\&e))$
  - $\sim a\&b$  same as  $(\sim a) \& b$
- Associativity is from left to right
  - $a | b | c$  same as  $(a | b) | c$
- As usual, precedence and associativity can be overridden using explicit  $($  and  $)$ , and  $|=$ ,  $\&=$ , and  $\wedge=$  are available

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Left and right shifts
  - $a \ll n$  same as  $a * 2^n$  modulo  $2^{\text{type width in bits}}$
  - $a \gg n$  same as  $a / 2^n$
  - Precedence lower than  $\sim$  but higher than  $|$ ,  $\&$ , and  $\wedge$
  - Beware: if  $n > \text{type width in bits}$ , or  $n < 0$ , result is undefined
- Applications
  - `isodd = (a&1)`; same as `isodd = a%2`;
  - `b&255` same as `b%256`
  - `a | 15` same as `(a/16)*16 + 15`
- You have to think in base 2 to get why and if it works
  - Think of the examples above ... did you get the pattern?
  - 256 is  $2^8$  and 255 is  $2^8 - 1$
  - 16 is  $2^4$  and 15 is  $2^4 - 1$
  - `a | 19` is NOT the same as `(a/20)*20 + 19`

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

```
enum boundary {  
    free_slip,  
    no_slip,  
    inflow,  
    outflow  
};
```

```
enum boundary leftside, rightside;
```

```
enum liquid {water, mercury} fluid; //may confuse readers
```

```
leftside = free_slip;
```

- A set of integer values represented by identifiers
  - Under the hood, it's an `int`
  - `free_slip` is an *enumeration constant* with value 0
  - `no_slip` is an enumeration constant with value 1
  - `inflow` is an enumeration constant with value 2
  - ...

# Choosing Values for Enumeration Constants

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

```
enum spokes {SpokesPerWheel = 36};
```

```
enum element {  
    hydrogen = 1,  
    helium,  
    carbon = 6,  
    oxygen = 8,  
    fluorine  
};
```

- Enumeration constants can be given a specified value
- When the enumeration constant value is not specified:
  - if it's the first in the declaration, gets the value 0
  - if it's not, gets (*value of the previous one*+1)
  - thus **helium** above gets 2, and **fluorine** gets 9
  - negative values can be used too
- A convenient way to give names to related integer constants

# Floating Types (as on Most CPUs)

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

Type	Conversion	Width (bits)	Size (bytes)
		Usual	Usual
<b>float</b>	<b>%f, %E, %G<sup>2</sup></b>	32	4
<b>double</b>	<b>%lf, %lE, %lG<sup>2</sup></b>	64	8
<b>long double</b>	<b>%Lf, %lE, %LG<sup>2</sup></b>	80 or 128	10 or 16
<b>float _Complex<sup>1</sup></b>	<i>none</i>	NA	8
<b>double _Complex<sup>1</sup></b>	<i>none</i>	NA	16
<b>long double _Complex<sup>1</sup></b>	<i>none</i>	NA	20 or 32

Constraints:

all **float** values must be representable in **double**

all **double** values must be representable in **long double**

1. C99
2. **%f** forces decimal notation, **%E** forces exponential decimal notation, **%G** chooses the one most suitable to the value

- New platform/compiler? Always check with **sizeof(type)**
- In practice, always in IEEE Standard binary format, but not a C Standard requirement
- **#include <complex.h>** and use **float complex**, **double complex**, and **long double complex**, if your program does not already uses the **complex** identifier

# #include <float.h>

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

Name	Meaning	Value
<b>FLT_EPSILON</b>	$\min\{x \mid 1.0 + x > 1.0\}$ in <b>float</b> type	$\leq 10^{-5}$
<b>DBL_EPSILON</b>	$\min\{x \mid 1.0 + x > 1.0\}$ in <b>double</b> type	$\leq 10^{-9}$
<b>LDBL_EPSILON</b>	$\min\{x \mid 1.0 + x > 1.0\}$ in <b>long double</b> type	$\leq 10^{-9}$
<b>FLT_DIG</b>	decimal digits of precision in <b>float</b> type	$\geq 6$
<b>DBL_DIG</b>	decimal digits of precision in <b>double</b> type	$\geq 10$
<b>LDBL_DIG</b>	decimal digits of precision in <b>long double</b> type	$\geq 10$
<b>FLT_MIN</b>	minimum normalized positive number in <b>float</b> range	$\leq 10^{-37}$
<b>DBL_MIN</b>	minimum normalized positive number in <b>long</b> range	$\leq 10^{-37}$
<b>LDBL_MIN</b>	minimum normalized positive number in <b>long double</b> range	$\leq 10^{-37}$
<b>FLT_MAX</b>	maximum finite number in <b>float</b> range	$\geq 10^{37}$
<b>DBL_MAX</b>	maximum finite number in <b>long</b> range	$\geq 10^{37}$
<b>LDBL_MAX</b>	maximum finite number in <b>long double</b> range	$\geq 10^{37}$
<b>FLT_MIN_10_EXP</b>	minimum $x$ such that $10^x$ is in <b>float</b> range and normalized	$\leq -37$
<b>DBL_MIN_10_EXP</b>	minimum $x$ such that $10^x$ is in <b>double</b> range and normalized	$\leq -37$
<b>LDBL_MIN_10_EXP</b>	minimum $x$ such that $10^x$ is in <b>long double</b> range and normalized	$\leq -37$
<b>FLT_MAX_10_EXP</b>	maximum $x$ such that $10^x$ is in <b>float</b> range and finite	$\geq 37$
<b>DBL_MAX_10_EXP</b>	maximum $x$ such that $10^x$ is in <b>double</b> range and finite	$\geq 37$
<b>LDBL_MAX_10_EXP</b>	maximum $x$ such that $10^x$ is in <b>long double</b> range and finite	$\geq 37$

- Use them to make code more portable across platforms
- New platform/compiler? Always check values
- “Normalized”? Yes, IEEE Standard allows for even smaller values, with loss of precision, and calls them “denormalized”
- “Finite”? Yes, IEEE Standard allows for infinite values

# Floating Literal Constants

## Arithmetic

Integers

Floating

Expressions

Mixing Types

## Aggregate

Structures

Defining Types

Arrays

Storage & C.

More Arrays

- Need something to distinguish them from integers
  - Decimal notation: `1.0`, `-17.`, `.125`, `0.22`
  - Exponential decimal notation: `2E19` ( $2 \times 10^{19}$ ), `-123.4E9` ( $-1.234 \times 10^{11}$ ), `.72E-6` ( $7.2 \times 10^{-7}$ )
- They have type **double** by default
  - Use suffixes **F** to make them **float** or **L** to make them **long double**
  - Lowercase will do as well, but `l` is easy to misread as `1`
- Never write `charge = protons*1.602176487E-19;`
  - `#define UNIT_CHARGE 1.602176487E-19`
  - or declare:
 

```
const double UnitCharge = 1.602176487E-19;
```
  - and use them in the code to make it readable
  - it will come handier when more precise measurements will be available

## Arithmetic

Integers  
 Floating  
 Expressions  
 Mixing Types

## Aggregate

Structures  
 Defining Types  
 Arrays  
 Storage & C.  
 More Arrays

Function/Macro	Returns
<b>HUGE_VAL</b> <sup>1</sup>	largest positive finite value
<b>INFINITY</b> <sup>1</sup>	positive infinite value
<b>NAN</b> <sup>1</sup>	IEEE quiet NaN (if supported)
<b>double fabs</b> (double <i>x</i> ),	$ x $ ,
<b>double copysign</b> (double <i>x</i> , double <i>y</i> ) <sup>1</sup>	if <i>y</i> ≠ 0 returns $ x y/ y $ else returns $ x $
<b>double floor</b> (double <i>x</i> ), <b>double ceil</b> (double <i>x</i> ), <b>double trunc</b> (double <i>x</i> ) <sup>1</sup> , <b>double round</b> (double <i>x</i> ) <sup>1</sup>	$\lfloor x \rfloor$ , $\lceil x \rceil$ , if <i>x</i> > 0 returns $\lfloor x \rfloor$ else returns $\lceil x \rceil$ , nearest <sup>2</sup> integer to <i>x</i>
<b>double fmod</b> (double <i>x</i> , double <i>y</i> ),	<i>x</i> mod <i>y</i> (same sign as <i>x</i> )
<b>double fdim</b> (double <i>x</i> , double <i>y</i> ) <sup>1</sup>	if <i>x</i> > <i>y</i> returns <i>x</i> - <i>y</i> else returns 0
<b>double nextafter</b> (double <i>x</i> , double <i>y</i> ) <sup>1</sup>	next representable value after <i>x</i> toward <i>y</i>
<b>double fmin</b> (double <i>x</i> , double <i>y</i> ) <sup>1</sup>	$\min\{x, y\}$
<b>double fmax</b> (double <i>x</i> , double <i>y</i> ) <sup>1</sup>	$\max\{x, y\}$
1. C99 2. If <i>x</i> is halfway, returns the farthest from 0	

- **#include <math.h>**
- Before C99, there were no **fmin()** or **fmax()**
  - Preprocessor macros have been widely used to this aim
  - Use the new functions, instead
- More functions are available to manipulate values
  - Mostly in the spirit of IEEE Floating Point Standard
  - We encourage you to learn more about



## Arithmetic

Integers

Floating

Expressions

Mixing Types

## Aggregate

Structures

Defining Types

Arrays

Storage & C.

More Arrays

Functions	Return
<code>double sqrt(double x),</code> <code>double cbrt(double x)<sup>1</sup>,</code> <code>double pow(double x, double y),</code> <code>double hypot(double x, double y)<sup>1</sup></code>	$\sqrt{x},$ $\sqrt[3]{x},$ $x^y,$ $\sqrt{x^2 + y^2}$
<code>double sin(double x), double cos(double x),</code> <code>double tan(double x), double asin(double x),</code> <code>double acos(double x), double atan(double x)</code>	Trigonometric functions
<code>double atan2(double x, double y)</code>	Arc tangent in $(-\pi, \pi]$
<code>double exp(double x),</code> <code>double log(double x), double log10(double x),</code> <code>double expm1(double x)<sup>1</sup>, double log1p(double x)<sup>1</sup></code>	$e^x,$ $\log_e x, \log_{10} x,$ $e^x - 1, \log(x + 1)$
<code>double sinh(double x), double cosh(double x),</code> <code>double tanh(double x), double asinh(double x)<sup>1</sup>,</code> <code>double acosh(double x)<sup>1</sup>, double atanh(double x)<sup>1</sup></code>	Hyperbolic functions
<code>double erf(double x)<sup>1</sup></code>	error function: $\frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$
<code>double erfc(double x)<sup>1</sup></code>	$1 - \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$
<code>double tgamma(double x)<sup>1</sup>, double lgamma(double x)<sup>1</sup></code> 1. C99	$\Gamma(x), \log( \Gamma(x) )$

- Again, `#include <math.h>`

# double complex Math

## C99 & C11

### Arithmetic

Integers  
 Floating  
 Expressions  
 Mixing Types

### Aggregate

Structures  
 Defining Types  
 Arrays  
 Storage & C.  
 More Arrays

Function/Macro	Returns
<code>double complex CmplX(double x, double y)</code> <sup>1</sup>	$x + iy$ ,
<code>double complex cabs(double complex z),</code> <code>double complex carg(double complex z),</code> <code>double complex creal(double complex z),</code> <code>double complex cimag(double complex z),</code> <code>double complex conj(double complex z)</code>	$ z $ , Argument of $z$ (a.k.a. phase angle), Real part of $z$ , Imaginary part of $z$ , Complex conjugate of $z$
<code>double complex csqrt(double complex z),</code> <code>double complex cpow(double complex z, double complex w)</code>	$\sqrt{z}$ , $z^w$
<code>double complex cexp(double complex z),</code> <code>double complex clog(double complex z)</code>	$e^z$ , $\log_e z$
1. C11	

- To use them, `#include <complex.h>`
  - You'll also get:
    - `csin()`, `ccos()`, `ctan()`,
    - `casin()`, `cacos()`, `catan()`,
    - `csinh()`, `ccosh()`, `ctanh()`,
    - `casinh()`, `cacosh()`, `catanh()`
  - And `I` for the imaginary unit

## Arithmetic

Integers

Floating

Expressions

Mixing Types

## Aggregate

Structures

Defining Types

Arrays

Storage & C.

More Arrays

- Before C99, all functions were only for **doubles**
  - And automatic conversion of other types was applied
- But from 1999 C is really serious about floating point math
  - All functions exist also for **float** and **long double**
  - Same names, suffixed by **f** or **l**
  - Like **acosf()** for arccosine of a **float**
  - Or **cacosl()** for **long double complex**
  - Ditto for macros, like **HUGE\_VALF** or **CMPLXL()**
- If you find this annoying (it is!):
  - **#include <tgmath.h>**
  - and use everywhere, for all real and complex types, function names for **double** type
  - These are clever type generic processor macros, expanding to the function appropriate to the argument

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- A fundamental concept in C
  - A very rich set of operators
  - Almost everything is an expression
  - Even assignment to a variable
- C expressions are complicated
  - Expressions can have side effects
  - Not all subexpressions are necessarily computed
  - Except for associativity and precedence rules, order of evaluation of subexpressions is up to the compiler
  - Values of different type can be combined, and a result produced according to a rich set of rules
  - Sometimes with surprising consequences
- We'll give a simplified introduction
  - Subtle rules are easily forgotten
  - Relying on them makes the code difficult to read
  - When you'll find a puzzling piece of code, you can always look for a good manual or book

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Binary operators  $+$ ,  $-$ ,  $*$  (multiplication) and  $/$  have the usual meaning and behavior
- Unary operator  $-$  evaluates to the opposite of its operand
- Unary operator  $+$  evaluates to its operand
- Precedence
  - $-a * b + c / d$  same as  $((-a) * b) + (c / d)$
  - $-a + b$  same as  $(-a) + b$
- Associativity of binary ones is from left to right
  - $a + b + c$  same as  $(a + b) + c$
  - $a * b / c * d$  same as  $((a * b) / c) * d$
- Explicit  $($  and  $)$  override precedence and associativity
- Only for integer types,  $\%$  is the modulo operator ( $27\%4$  evaluates to 3), same precedence as  $/$

# Hitting Limits

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- All types are limited in range
- What about:
  - `INT_MAX + 1`? (too big)
  - `INT_MIN*3`? (too negative)
- Technically speaking, this is an arithmetic *overflow*
- And division by zero is a problem too
- For signed integer types, the Standard says:
  - behavior and results are unpredictable
  - i.e. up to the implementation
- For other types, the Standard says:
  - arithmetic on unsigned integers must be exact modulo  $2^{\text{type width}}$ , no overflow
  - with floating types, is up to the implementation (you can get `DBL_MAX`, or a NaN, or an infinity)
- Best practice: NEVER rely on behaviors observed with a specific architecture and/or compiler

# Assignment Operator

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Binary operator =
  - assigns the value of the right operand to the left operand
  - and returns the value of the right operand
  - thus  $a = b*2$  is an expression with value  $b*2$  and the side effect of changing variable  $a$
  - $a = b*2$ ; is an assignment statement
- The left operand must be something that can store a value
  - In C jargon, an *lvalue*
  - $a = 20$  is OK, if  $a$  is a variable
  - $20 = a$  is not
- Precedence is lowest (except for `,` operator) and associativity is from right to left
  - $a = b*2 + c$  same as  $a = (b*2 + c)$
  - $z = a = b*2 + c$  same as  $z = (a = (b*2 + c))$
- You'll read the latter form, particularly in `while ()` statements, but avoid writing it

## Arithmetic

Integers  
 Floating  
 Expressions  
 Mixing Types

## Aggregate

Structures  
 Defining Types  
 Arrays  
 Storage & C.  
 More Arrays

- Most binary operators offer useful shortcut forms:

Expression	Same as
<code>a += b</code>	<code>a = a + b</code>
<code>a -= b</code>	<code>a = a - b</code>
<code>a *= b</code>	<code>a = a*b</code>
<code>a /= b</code>	<code>a = a/b</code>
<code>a %= b</code>	<code>a = a%b</code>

- In heroic times, used to map some CPUs optimized instructions
- With nowadays optimizing compilers, only good to spare keystrokes
- You'll find them often, particularly in `for(;;)` statements



## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Pre-increment/decrement unary operators: `++` and `--`
  - `++i` same as `(i = i + 1)`
  - `--i` same as `(i = i - 1)`
- Post-increment/decrement unary operators: `++` and `--`
  - `i++` increments `i` content, but returns the original value
  - `i--` decrements `i` content, but returns the original value
- Operand must be an *lvalue*
- Precedence is highest
- Quite handy in `while ()` and `for (;;) statements`
- Easily becomes a nightmare inside expressions
  - Particularly when you change the code

# Order of Subexpressions Evaluation

## Arithmetic

Integers

Floating

Expressions

Mixing Types

## Aggregate

Structures

Defining Types

Arrays

Storage & C.

More Arrays

- `i` is an `int` type variable whose value is 5
  - `j = 4*i++ - 3*++i;`
  - `foo(++i, ++i);`
- Which value is assigned to `j`?
  - Could be
  - Or could as well be
- Which values are passed to `foo()`?
  - Could be `foo( , )`
  - Or could as well be `foo( , )`
- Order of evaluation of subexpressions is implementation defined!
- Ditto for order of evaluation of function arguments!
- NEVER! NEVER pre/post-in/de-crement the same variable twice in a single expression, or function call!

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Comparison operators
  - `==` (equal), `!=` (not equal), `>`, `<`, `>=`, `<=`
  - Compare operand values
  - Return `int` type 0 if evaluation is false, 1 if true
  - Precedence lower than arithmetic operators, higher than bitwise and logical operators
  - In doubt, add parentheses, but be sober
- Logical operators
  - `!` is unary NOT, `&&` is binary AND, `||` is binary OR
  - Zero operand are considered false, non zero ones true
  - Return `int` type 0 if comparison is false, 1 if true
  - Precedence of `!` just lower than `++` and `--`
  - `&&`, `||`: higher than `=` and friends
  - `!a&&b || a&&!b` means `((!a)&&b) || (a&&(!b))`
  - Again: in doubt, add parentheses, but be sober

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Some macros to tame floating point complexity
- `isfinite()`
  - True if argument value is finite
- `isinf()`
  - True if argument value is an infinity
- `isnan()`
  - True if argument value is a NaN
- And more, if you are really serious about floating point calculations
  - Mostly in the spirit of IEEE Floating Point Standard
  - Learn more about it, before using them

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- C99 defines integer type `_Bool`
  - Only guaranteed to store 0 or 1
  - Perfect for logical (a.k.a. boolean) expressions
  - Use it for “flag” variables, and to avoid surprises
  - Better yet, `#include <stdbool.h>`, and use type `bool`, and values `true` and `false`
- Watch your step!
  - Simply mistype `&` for `&&` or vice versa
  - Simply mistype `||` for `|`
  - You’ll discover, possibly after hours of debugging, that (bitwise arithmetic) `!=` (logical arithmetic)
- C99 offers a fix to this unfortunate choice
  - `#include <iso646.h>`
  - And use `not`, `or`, and `and` in place of `!`, `||` and `&&`

# Even More Side Effects

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Right operand of `||` and `&&` is evaluated after left one
- And is not evaluated at all if:
  - left one is found true for an `||`
  - left one is found false for an `&&`
- Beware of “short circuit” evaluation...
  - ... if the right operand is an expression with side effects!
  - A life saver in preprocessor macros and a few more cases
  - But makes your code less readable
  - Use nested `if ()` whenever you can
- *logical-expr ? expr1 : expr2*
  - *expr1* is only evaluated if *logical-expr* is true
  - *expr2* is only evaluated if *logical-expr* is false
  - Again, is a life saver in preprocessor macros
  - But in normal use an `if ()` is more readable

# Mixing Types in Expressions

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- C allows for expressions mixing any arithmetic types
  - A result will always be produced
  - Whether this is the result you expect, it's another story
- Broadly speaking, the base concept is clear
- For each binary operator in the expression, in order of precedence and associativity:
  - if both operands have the same type, fine
  - otherwise, operand with narrower range is converted to type of other operand
- OK when mixing floating types
  - The wider range includes the narrower one
- OK when mixing signed integer types
  - The wider range includes the narrower one
- OK even when mixing unsigned integer types
  - The wider range includes the narrower one

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- For the assignment operator:
  - if both operands have the same type, fine
  - otherwise, right operand is converted to left operand type
  - if the value cannot be represented in the destination type, it's an overflow, and you are on your own
  
- We said: in order of precedence and associativity
  - if **a** is a type `long long int` variable, and **b** is a 32 bits wide `int` type variable and contains value `INT_MAX`, in:  
`a = b*2`  
multiplication will overflow
  - and in:  
`a = b*2 + 1LL`  
multiplication will overflow too
  - while:  
`a = b*2LL + 1`  
is OK



## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Think of mixing floating and integer types
  - Floating types have wider range
  - But not necessarily more precision
  - A 32 bits `float` has fewer digits of precision than a 32 bits `int`
  - And a 64 bits `double` has fewer digits of precision than a 64 bits `int`
  - The result could be smaller than expected
- Think of mixing signed and unsigned integer types!
  - Negative values cannot be represented in unsigned types
  - Half of the values representable in an unsigned type, cannot be represented in a signed type of the same width
  - So, you are in for implementation defined surprises!
  - And Standard rules are quite complicated
  - We spare you the gory details, simply don't do it!

# Cast Your Subexpressions

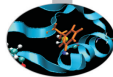
## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- *(type)*
  - Unsurprisingly, it's an operator
  - Precedence just higher than multiplication, right-to-left associative
  - Use it like `(unsigned long)(sig + ned)`
- Casting let you override standard conversion rules
  - In previous example, you could use it like this:  
`a = (long long int)b*2 + 1`
- Type casting is not magic
  - Just instructs compiler to apply the conversion you need
  - Only converts values, not type of variables you assign to
- Do not abuse it
  - Makes codes unreadable
  - Could be evidence of design mistakes
  - Or that your C needs a refresh

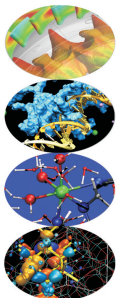


# Scientific and Technical Computing in C

Stefano Tagliaventi    Luca Ferraro

CINECA Roma - SCAI Department

Rome, 3-5 February 2016



## Arithmetic

- Integers
- Floating
- Expressions
- Mixing Types

## Aggregate

- Structures
- Defining Types
- Arrays
- Storage & C.
- More Arrays

### 1 Arithmetic Types and Math

- ### 2 Aggregate Types
- Structure Types
  - Defining New Types
  - Arrays
  - Storage Classes, Scopes, and Initializers
  - Arrays & Functions

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

```
struct vect3D {
    double x, y, z;
};

struct vect3D va, vb;

// REMINDER: I have to make vcross() more efficient!
struct vect3d vcross(struct vect3D u, struct vect3D v) {
    struct vect3D c;

    c.x = u.y*v.z - u.z*v.y;
    c.y = u.z*v.x - u.x*v.z;
    c.z = u.x*v.y - u.y*v.x;

    return c;
}

//...
vc = vcross(va, vb);
```

- Aggregates a single type from named, typed components (a.k.a. members)
- The `vect3D` tag must be unique among structure tags
- `struct` components can be independently accessed using the `.` binary operator

# structs Are Flexible

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

```
struct ion {  
    struct vect3D r; // position  
    struct vect3D v; // velocity  
    enum element an; // atomic number  
    int q; // in units of elementary charges  
};  
  
struct ion a;  
//...  
a.r.x += dt*a.v.x; // very low order in time...
```

- **struct** components can be inhomogeneous
- And they can also be **structs**, of course
  - To access nested **struct** components, chain `.` expressions
- Best practice: order components by decreasing size
  - You'll get better performances
  - To know, you can use `sizeof()` operator on any type

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- **structs** are widely used in C Standard Library
- Like in **struct tm**, below, defined in **time.h**
  - Used to convert from/to internal time representation **time\_t**

```
struct tm {  
    int tm_sec; // seconds after the minute [0, 60]  
    int tm_min; // minutes after the hour [0, 59]  
    int tm_hour; // hours since midnight [0, 23]  
    int tm_mday; // day of the month [1, 31]  
    int tm_mon; // months since January [0, 11]  
    int tm_year; // years since 1900  
    int tm_wday; // days since Sunday [0, 6]  
    int tm_yday; // days since January 1 [0, 365]  
    int tm_isdst; // Daylight Saving Time flag  
};
```

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

```
typedef struct vect3D position, velocity;  
  
typedef enum element element; // let's spare keystrokes  
  
typedef int charge;           // I'll maybe switch to short or signed char  
  
typedef struct ion {  
    position r;  
    velocity v;  
    element an;  
    charge q;  
} ion;  
  
ion a;
```

- **typedef** turns a normal declaration into a declaration of a new type (as usual, a legal identifier)
- The new type can be used as the native ones
  - Great to save keystrokes
  - Even better to write self-documenting code
  - Shines in hiding and factoring out implementation details
- **struct** tags and type identifiers belong to separate sets



## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- **typedef** is widely used in C Standard Library
- Mostly to abstract details that may differ among implementations
- E.g. **size\_t** from **stddef.h**
  - Type of value returned by **sizeof()**
  - Different platforms allow for different memory sizes
  - **size\_t** must be “**typedefed**” to an integer type able to represent the maximum possible variable size allowed by the implementation
- E.g. **clock\_t** from **time.h**
  - Type of value returned by **clock()**
  - Cast it to **double**, divide by **CLOCK\_PER\_SEC**, ...
  - and you’ll know the CPU time in seconds used by your program from its beginning

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- `some_type a[n];`
  - declares a collection of  $n$  variables of type *some\_type*
  - the variables (a.k.a. elements) are laid out contiguously in memory
  - each element can be read or written using the syntax `a[integer indexing expression]`
  - first element is `a[0]`, second one is `a[1]`, last one is `a[n-1]`
- You can't work on an array as a whole
  - Use array elements (if allowed...) in expressions and assignments
- There is no bound checking!
  - Use a negative index, or an index too big, and you are accessing something else, if any
  - Compiler options to (very slowly) check every access
- A common mistake:
  - to access from `double a[1]` to `double a[n]`
  - Fortran programmers beware!

# Arrays of(Arrays of(Arrays of(...)))

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- C has no concept of multidimensional arrays
- But array is a regular C type (you can even `sizeof(double[150])`)
- Thus, arrays of arrays can be declared
  - A simple, practical abstraction
  - Very annoying to Fortran or Matlab programmers
- `int a[12][31];`
  - declares an array of 12 elements
  - and each element is itself an array of 31 `ints`
- `double b[130][260][260];`
  - declares an array of 130 elements
  - and `b[37]` is itself an array of 260 elements
  - and `b[37][201]` is again an array of 260 `doubles`
- By the way, you can also use `sizeof(b)`, it works

## Arithmetic

- Integers
- Floating
- Expressions
- Mixing Types

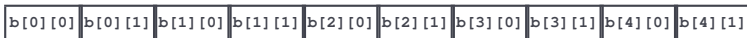
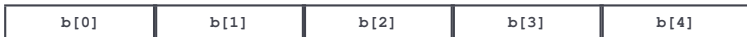
## Aggregate

- Structures
- Defining Types
- Arrays
- Storage & C.
- More Arrays

```
int a[10];
```



```
int b[5][2];
```



# A Very Important Digression

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Storage duration
  - To make it simple, the life time of a variable
  - Also influences the part of memory where it's allocated
- Scope
  - The region where a variable or function is accessible, a.k.a. "visible"
- Qualifiers
  - The value in a **const** variable cannot be changed
  - There are more, but we'll not discuss them
- Initializers
  - Values assigned to a variable at declaration

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- A variable can be
  - Automatic: it can be created when needed, and destroyed when not needed anymore
  - Static: it persists for the whole duration of the program
- Variables declared outside of any functions (i.e. at file scope) are static
- By default, are automatic:
  - all variables declared inside a compound statement
  - function parameters
- The default can be overridden using **static**
- Functions are static too, because to call them you need their code to persist in memory

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- By default, variables declared at file scope and functions are **extern**
  - i.e. visible to the linker, and to the whole program
  - Unless you declare them to be **static** only
- Variables declared at file scope and functions are visible to all blocks in the same source file
- Variables declared in a block are only visible in the block and in all scopes it encloses
  - Unless you declare them **extern**
  - But in most cases that's a symptom of bad design
- A variable declared in a block hides anything declared with the same name in enclosing scopes

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- The content of an automatic variable is *uninitialized* until the variable is assigned a value
- *Uninitialized* is a polite form for "unpredictable rubbish"
- **double f = 2.5;** is a practical shorthand for:

```
double f;  
f = 2.5;
```

- Expressions can be used as initializers, as long as they can be computed at that point:

```
double pi = acos(-1.0);  
double pihalf = pi/2.0;
```

is legal, while the following:

```
double pihalf = pi/2.0;  
double pi = acos(-1.0);
```

obviously is not



## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- **structs** can be initialized too, as in:  

```
struct vect3D v = {0.0, 1.0, 0.0};
```
- Same for arrays, as in:  

```
float rot[2][2] = {{0.0, -1.0}, {1.0, 0.0}};
```
- `{0.0, 1.0, 0.0}` and `{{0.0, -1.0}, {1.0, 0.0}}` are said *compound literals*
- By default, static variables are initialized to 0
- But they can be initialized to different values
- Expressions can also be used, with some restrictions
  - For a static variable, initialization expression must be computed at compile time
  - I.e. it must be a *constant expression*, containing only constants
  - No variables, no function calls are permitted

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Static arrays must be dimensioned with constant expressions
- Before C99, this was true for automatic arrays too
  - So to use an array in a function, you had to dimension it for the largest possible amount of work
  - A waste of memory and error prone
- C99 has a much better way
- Variable length arrays
  - Arrays whose size is unknown until run time
  - Automatic arrays can have their dimension specified by a nonconstant expression
  - Every time execution enters the block, the expression is evaluated
  - And the array size is determined, up to exit from the block

# Arrays as Function Arguments

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Arrays can be huge
  - And usually are, in S&T computing
  - Passing them by value would be too costly
- Moreover, arrays cannot be used in assignments
  - Thus a function cannot return an array
- The solution
  - The address of the array is passed to a function
  - And elements can be accessed by it
  - (Later on, you'll understand how)
- This allows elements to be assigned to
  - Thus a function has a way to “return” an array result
  - A mixed blessing: allows changes to happen by mistake
- Best practice: declare an array parameter **const** if your only intent is reading its elements

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Let's write a function to average an array of **doubles**
- And make it generic in the array length
- Variable length array parameters come to the rescue

```
double avg(int n, const double a[n]) {  
    int i;  
    double sum = 0.0;  
  
    for (i=0; i<n; ++i)  
        sum += a[i];  
  
    return sum/n;  
}
```

Beware: `double avg(double a[n], int n)` does not work!

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Before C99, there were no VLAs
- The solution was simple
  - Compiler just uses type size to find the right element
  - No bounds checking, no bound needed
- Many still write that way: it's equivalent, but less readable

```
double avg(int n, const double a[]) {  
    int i;  
    double sum = 0.0;  
  
    for (i=0; i<n; ++i)  
        sum += a[i];  
  
    return sum/n;  
}
```

# Calling `avg()`

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- New or old style, simply pass array dimension and name
- If `avg()` is written using VLAs, pedantic compilers may give a warning on function call, even if it's correct: they are wrong, check with Standard document or good book

```
double mydata[N];  
double mydata_avg;  
  
// read or compute N doubles into mydata[]  
  
mydata_avg = avg(N, mydata);
```

# Averaging Arrays of 5 Elements

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Let's write a function to average arrays of 5 **doubles**
- And make it generic, as usual
- Again, VLA parameters come to the rescue

```
void avg5(int n, const double a[n][5], double b[5]) {  
    int i, j;  
  
    for (j=0; j<5; ++j)  
        b[j] = 0;  
  
    for (i=0; i<n; ++i)  
        for (j=0; j<5; ++j)  
            b[j] += a[i][j];  
  
    for (j=0; j<5; ++j)  
        b[j] /= n;  
}
```

Notice: this order of loops nesting gives faster execution

# Averaging Arrays of 5 Elements, the Old Way

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Let's write a function to average arrays of 5 **doubles**
- And make it generic, as usual
- Again, do not specify first bound
- Again, it's equivalent

```
void avg5(int n, const double a[][5], double b[5]) {  
    int i, j;  
  
    for (j=0; j<5; ++j)  
        b[j] = 0;  
  
    for (i=0; i<n; ++i)  
        for (j=0; j<5; ++j)  
            b[j] += a[i][j];  
  
    for (j=0; j<5; ++j)  
        b[j] /= n;  
}
```



# Calling `avg5 ()`

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- New or old style, simply pass array dimension and name
- If `avg5 ()` is written using VLAs, pedantic compilers may give a warning on function call, even if it's correct: they are wrong, check with Standard document or good book

```
double mydata[N][5];  
double mydata_avg[5];  
  
// read or compute N 5-uples of doubles into mydata[]  
  
avg5(N, mydata, mydata_avg);
```

# Averaging Arrays of Arbitrary Length

- Let's generalize the average to set of  $m$  numbers
- And make it generic, as usual
- Again, VLA parameters come to the rescue

```
void avg(int n, int m, const double a[n][m], double b[m]) {  
  
    int i, j;  
  
    for (j=0; j<m; ++j)  
        b[j] = 0;  
  
    for (i=0; i<n; ++i)  
        for (j=0; j<m; ++j)  
            b[j] += a[i][j];  
  
    for (j=0; j<m; ++j)  
        b[j] /= n;  
  
}
```

Notice: this order of loops nesting gives faster execution

# Calling Generic `avg()`

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Again, simply pass array dimension and name
- Using casts for arrays of doubles
- If `avg()` is written using VLAs, pedantic compilers may give a warning on function call, even if it's correct: they are wrong, check with Standard document or good book

```
double mydata1[N][12];  
double mydata1_avg[12];  
double mydata2[N][7];  
double mydata2_avg[7];  
double mydata3[N][1];  
double mydata3_avg[1];  
double mydata4[N];  
double mydata4_avg[1];  
  
// read or compute N 12-uples of doubles into mydata1[]  
// read or compute N 7-uples of doubles into mydata2[]  
// read or compute N 1-uples of doubles into mydata3[]  
// read or compute N doubles into mydata4[]  
  
avg(N, 12, mydata1, mydata1_avg);  
avg(N, 7, mydata2, mydata2_avg);  
avg(N, 1, mydata3, mydata3_avg);  
avg(N, 1, (double [N][1])mydata4, mydata4_avg);
```

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Let's write a function to compute the trace of a matrix of **doubles**
- And make it generic in the matrix size
- Again, variable length array parameters come to the rescue
- Again, you may get warnings on calls, and they could prove wrong

```
double tr(int n, const double a[n][n]) {  
    int i;  
    double sum = 0.0;  
  
    for (i=0; i<n; ++i)  
        sum += a[i][i];  
  
    return sum;  
}
```

Beware: compiler will not check the array dimensions match!

# Matrix Algebra, the Old Way

## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

- Before C99, there were no VLAs
- The solution was not that simple...
  - Only the 'first dimension' of an array parameter could be left unspecified at compile time
- To understand the solution, you have to learn more



## Arithmetic

Integers  
Floating  
Expressions  
Mixing Types

## Aggregate

Structures  
Defining Types  
Arrays  
Storage & C.  
More Arrays

These slides are ©CINECA 2016 and are released under the Attribution-NonCommercial-NoDerivs (CC BY-NC-ND) Creative Commons license, version 3.0.

Uses not allowed by the above license need explicit, written permission from the copyright owner. For more information see:

<http://creativecommons.org/licenses/by-nc-nd/3.0/>

Slides and examples were authored by:

- Michela Botti
- Federico Massaioli
- Luca Ferraro
- Stefano Tagliaventi